



# Towards a seamless Integration of CAD and Simulation

## *Introduction*

**Multi-scale fracture and model order reduction** Pierre Kerfriden, Lars Beex, Jack Hale, Olivier Goury, Daniel Alves Paladim, Elisa Schenone, Davide Baroli, Thanh Tung Nguyen

**Advanced discretisation techniques** Danas Sutula, Xuan Peng, Haojie Lian, Peng Yu, Qingyuan Hu, Sundararajan Natarajan, Nguyen-Vinh Phu

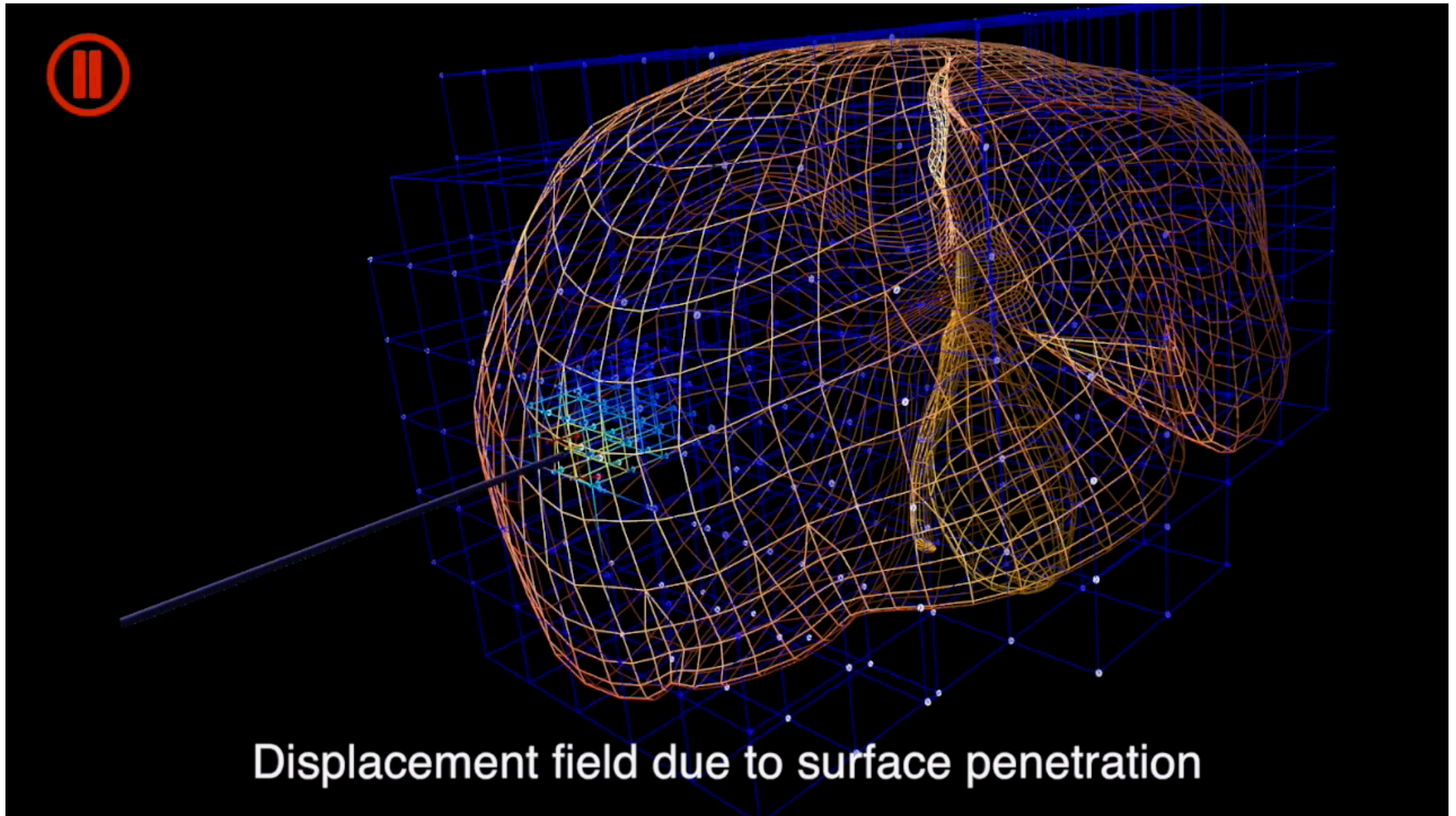
**Error estimation** Pierre Kerfriden, Satyendra Tomar, Daniel Alves Paladim, Andrés Gonzalez Estrada

**Biomechanics applications** Alexandre Bilger, Hadrien Courtecuisse, Bui Huu Phuoc

and all the others!

CISM Course, Udine, Italy, 2017 June 5-9  
Stéphane P.A. Bordas [stephane.bordas@alum.northwestern.edu](mailto:stephane.bordas@alum.northwestern.edu) <http://legato-team.eu>  
Organised by Gernot Beer & Stéphane Bordas

# Computer-assisted surgery



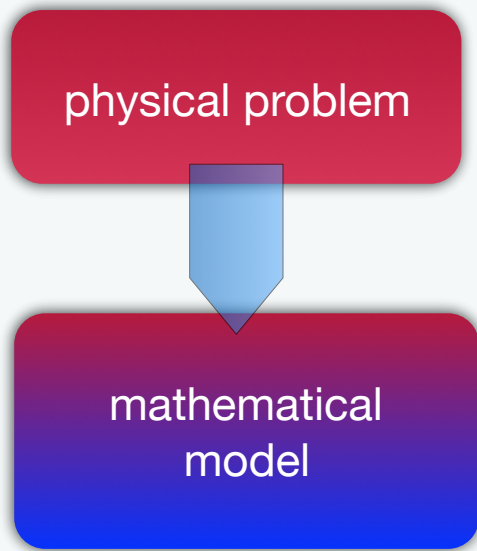
## Needle insertion in the liver

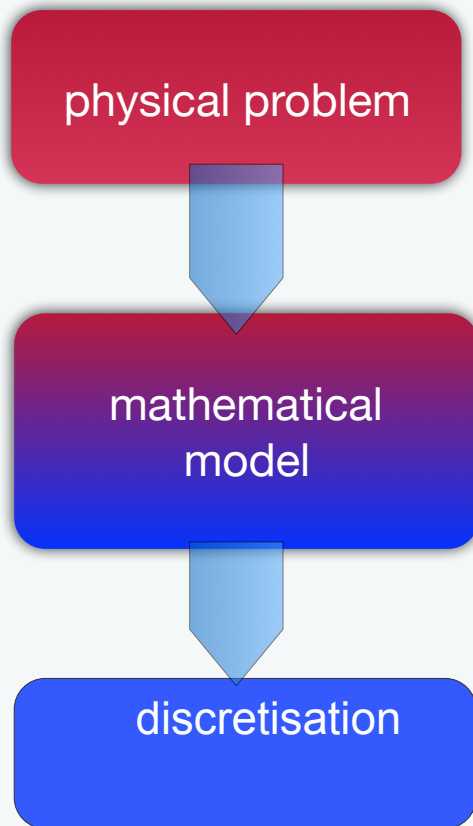




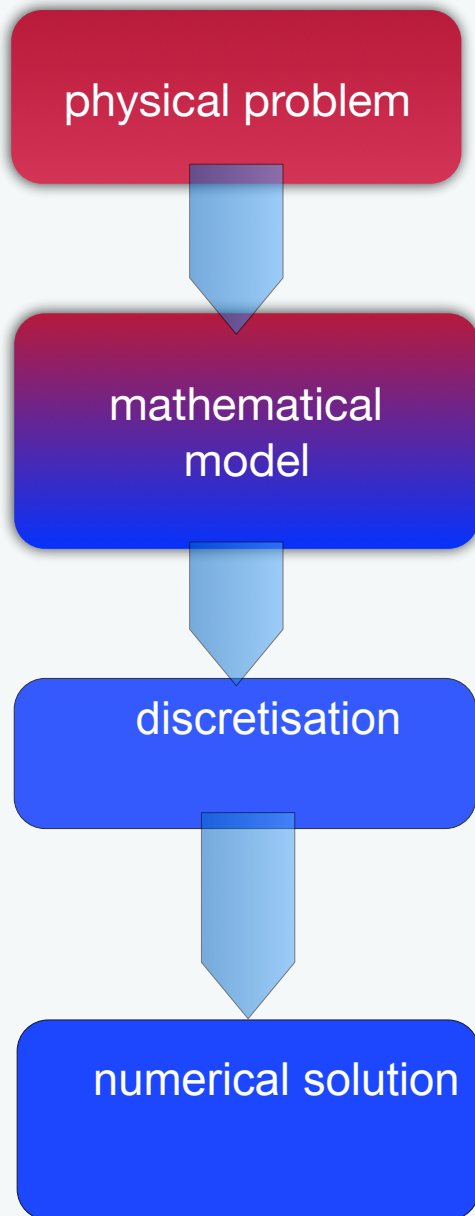
physical problem



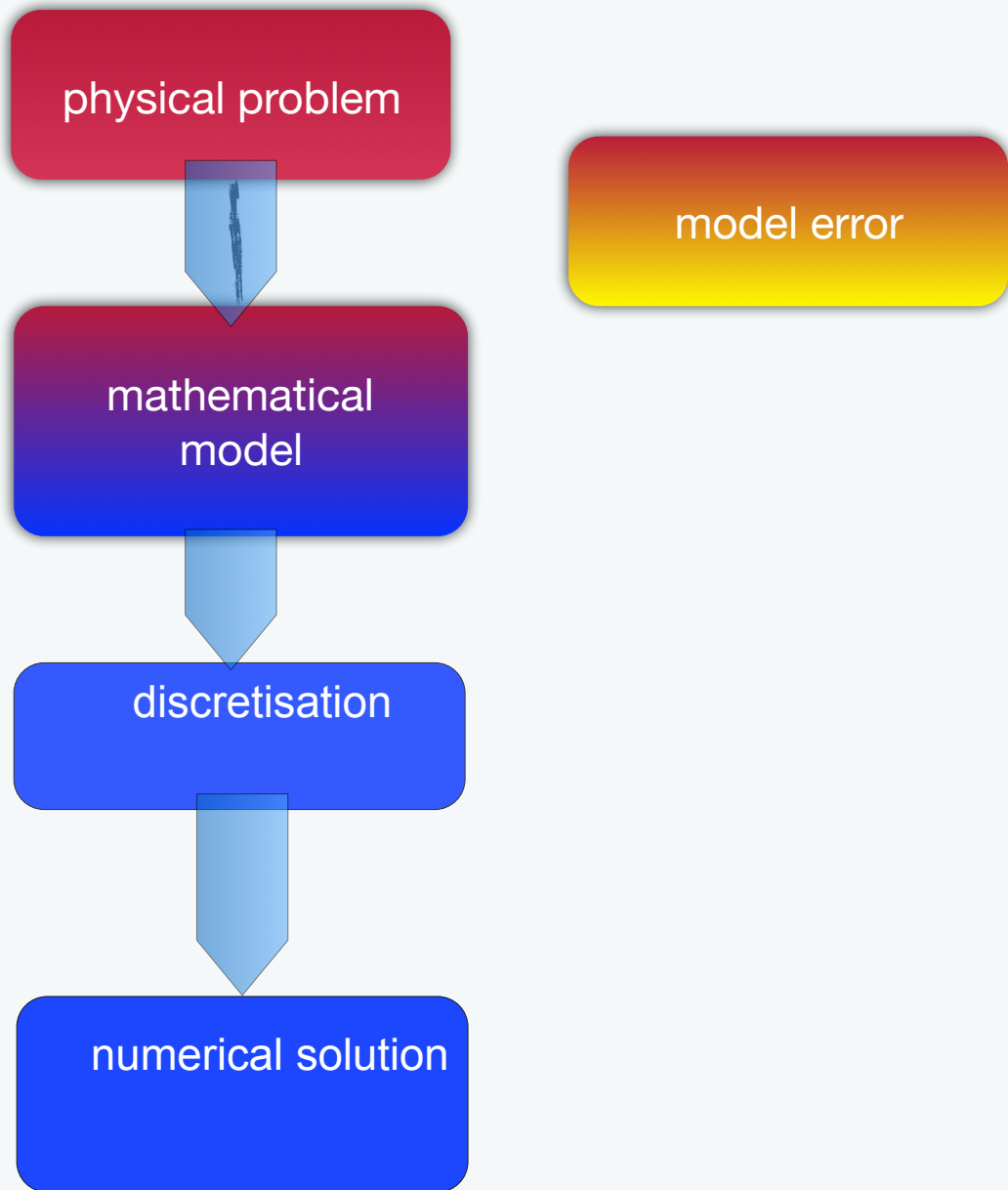






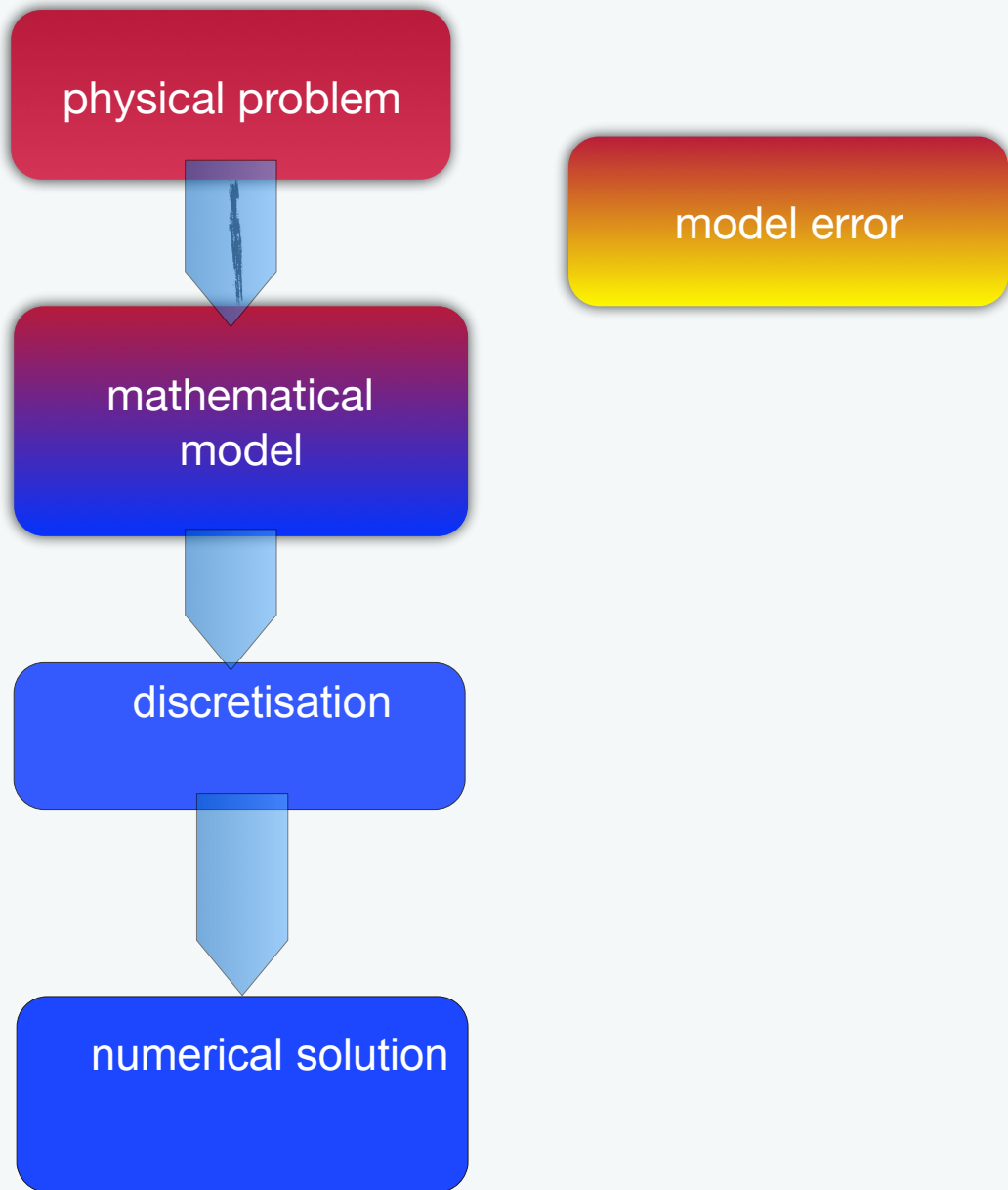


# Modelling and simulation

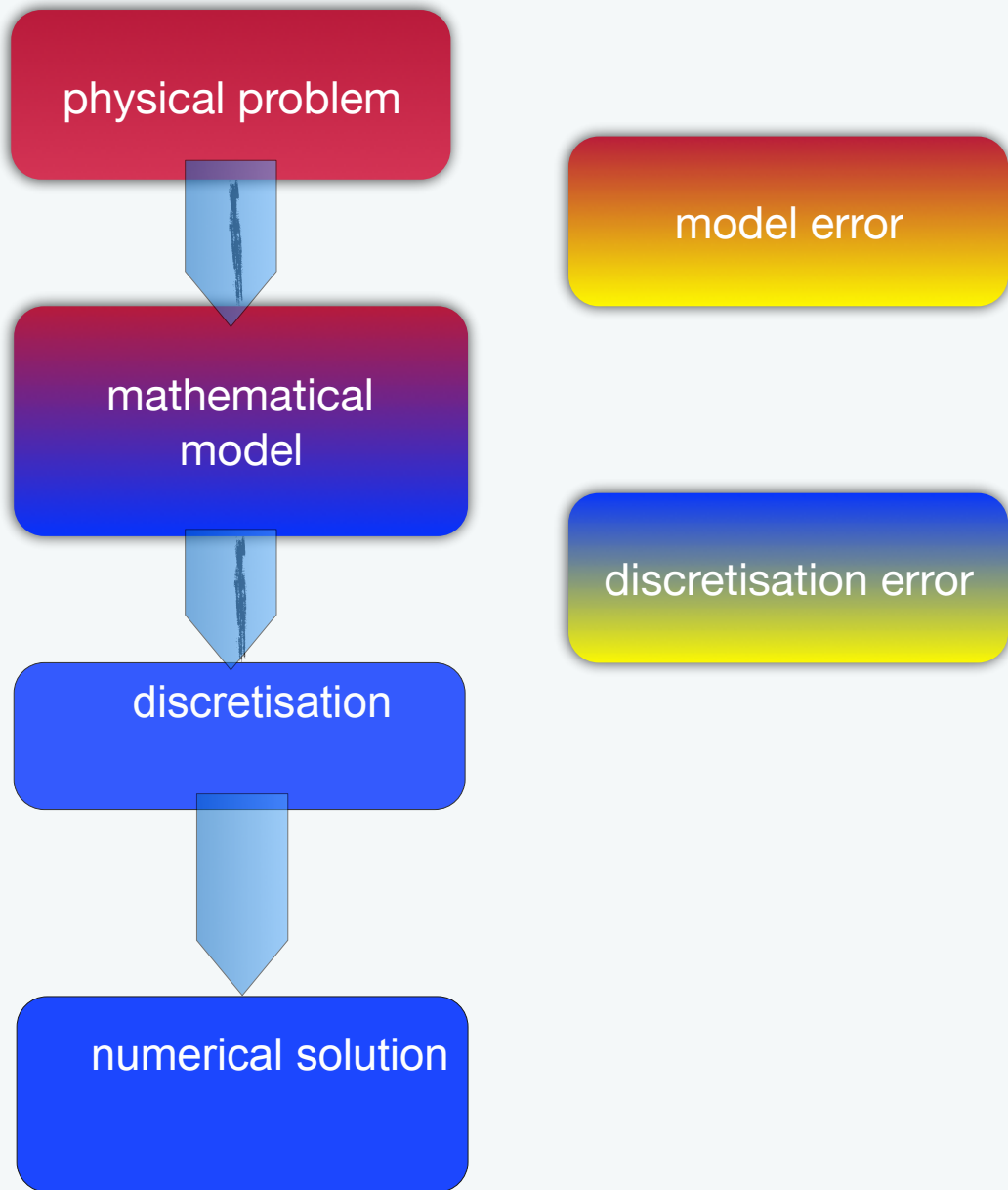




# Modelling and simulation

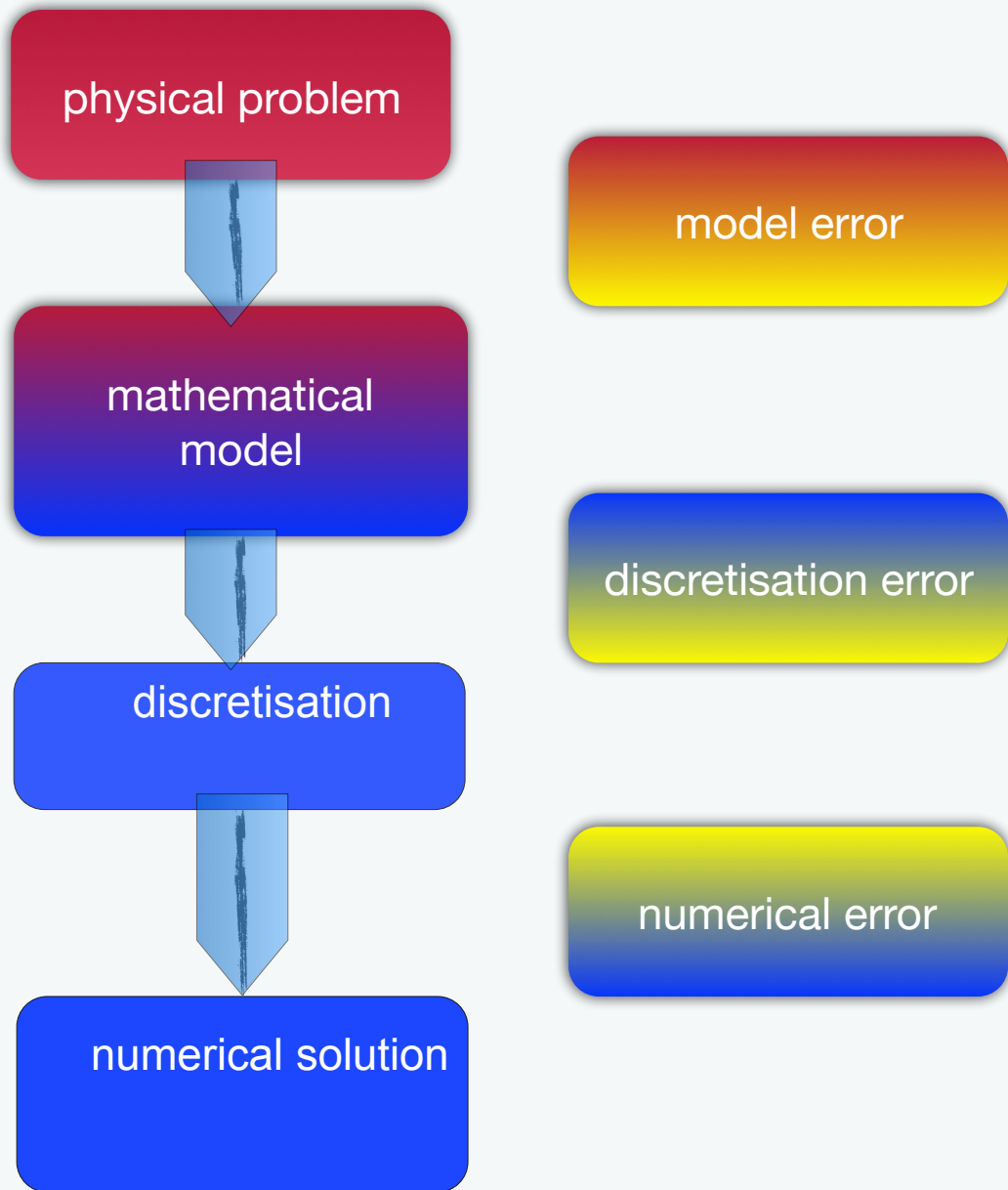


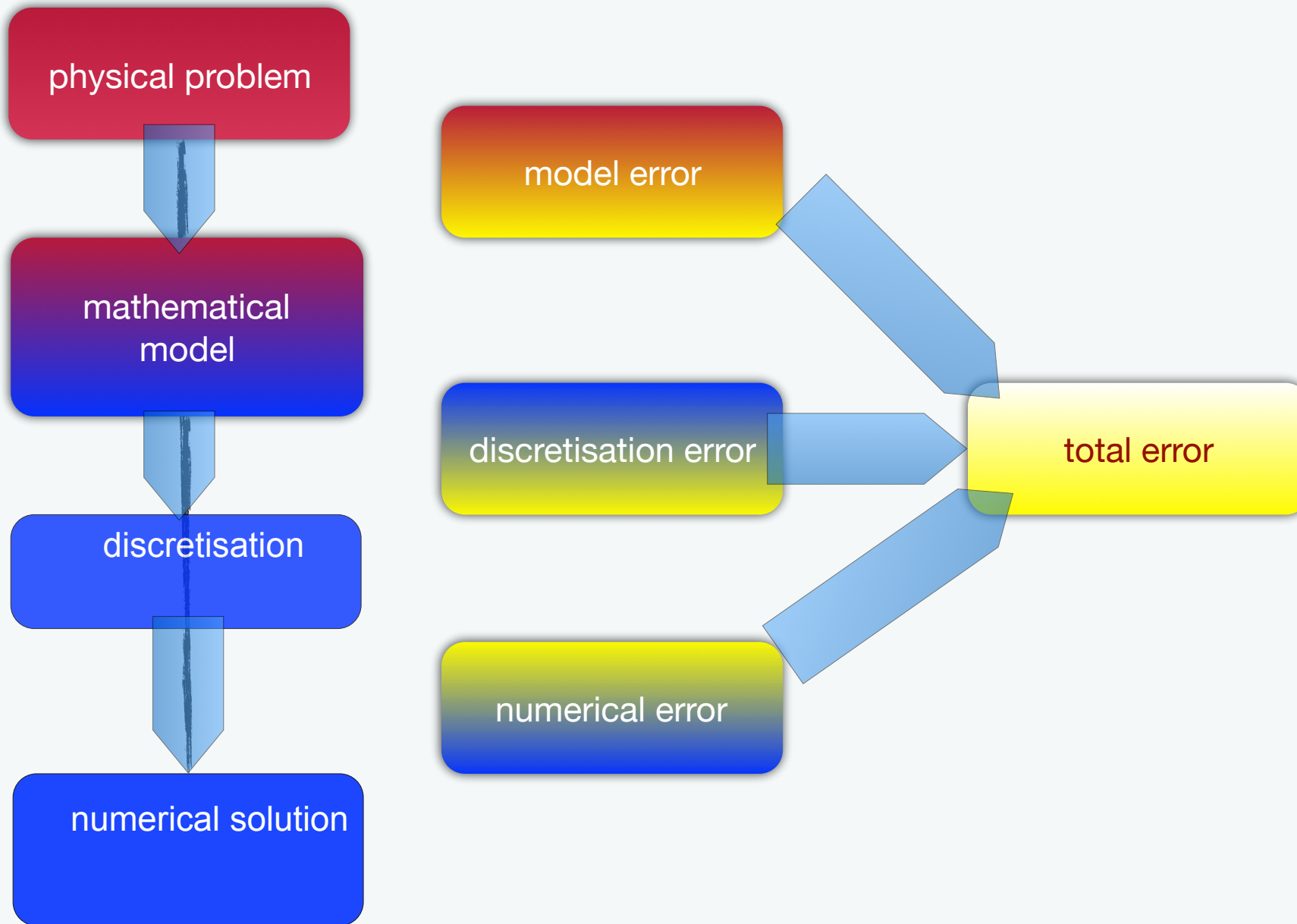
# Modelling and simulation





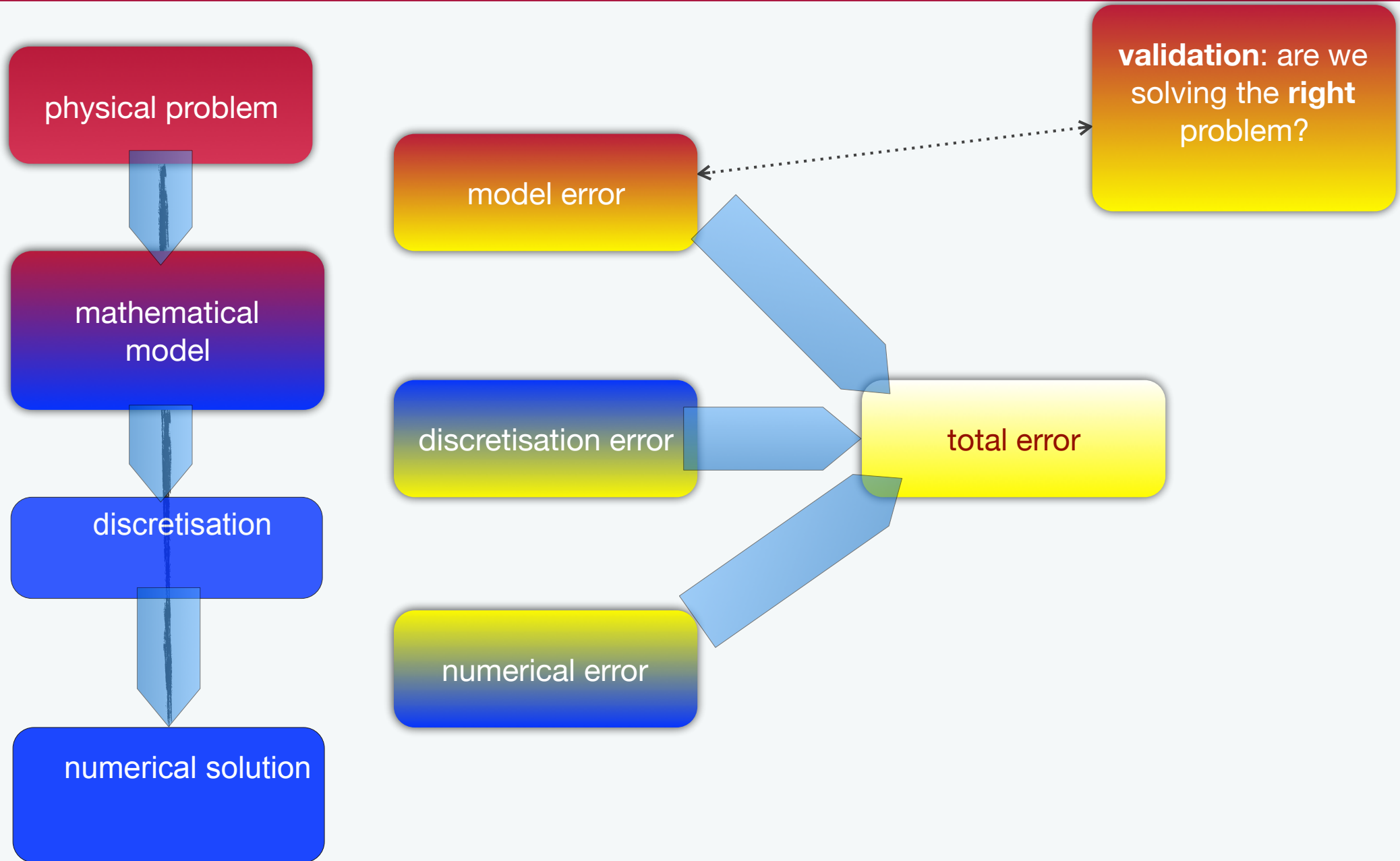
# Modelling and simulation



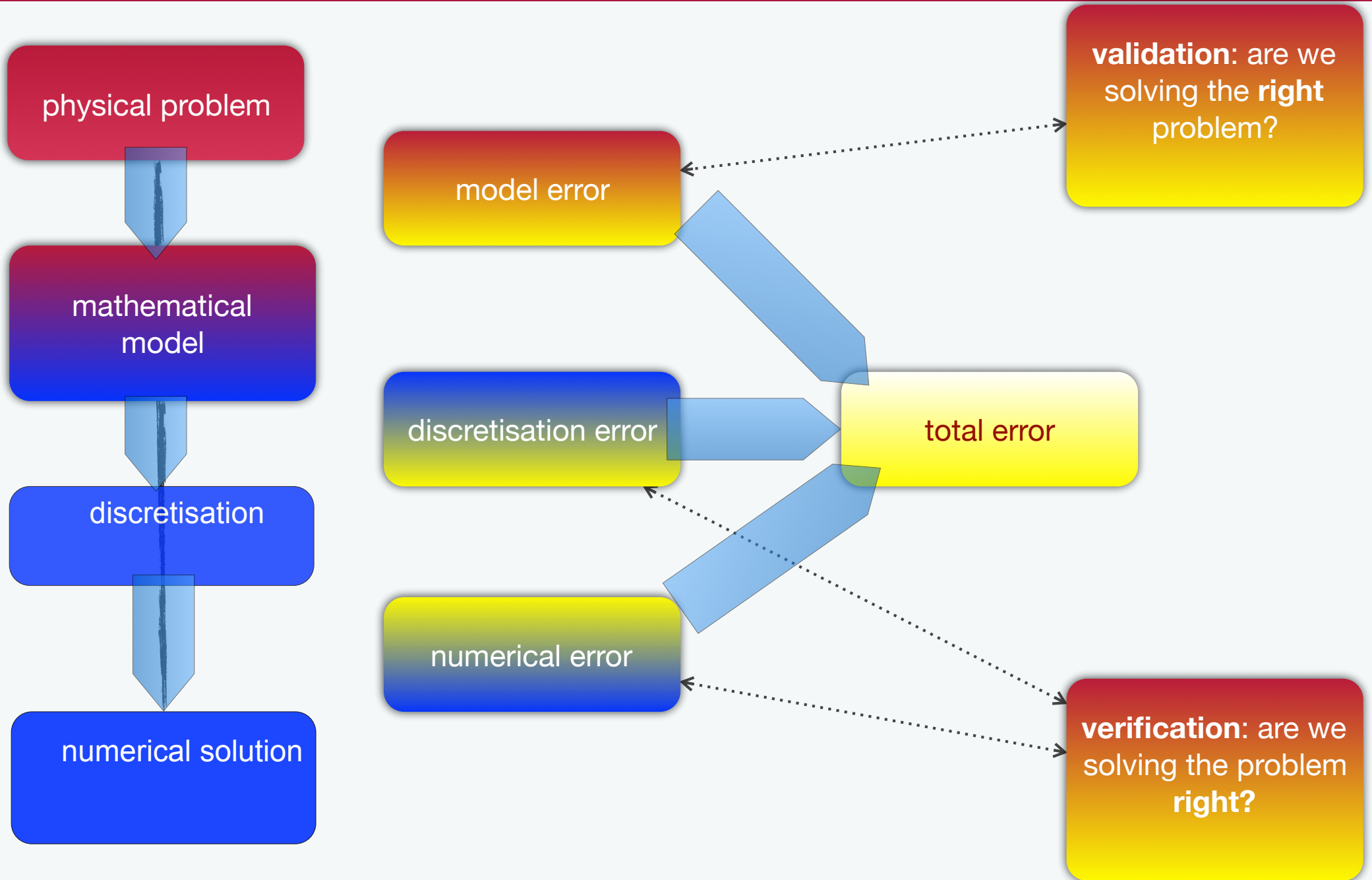




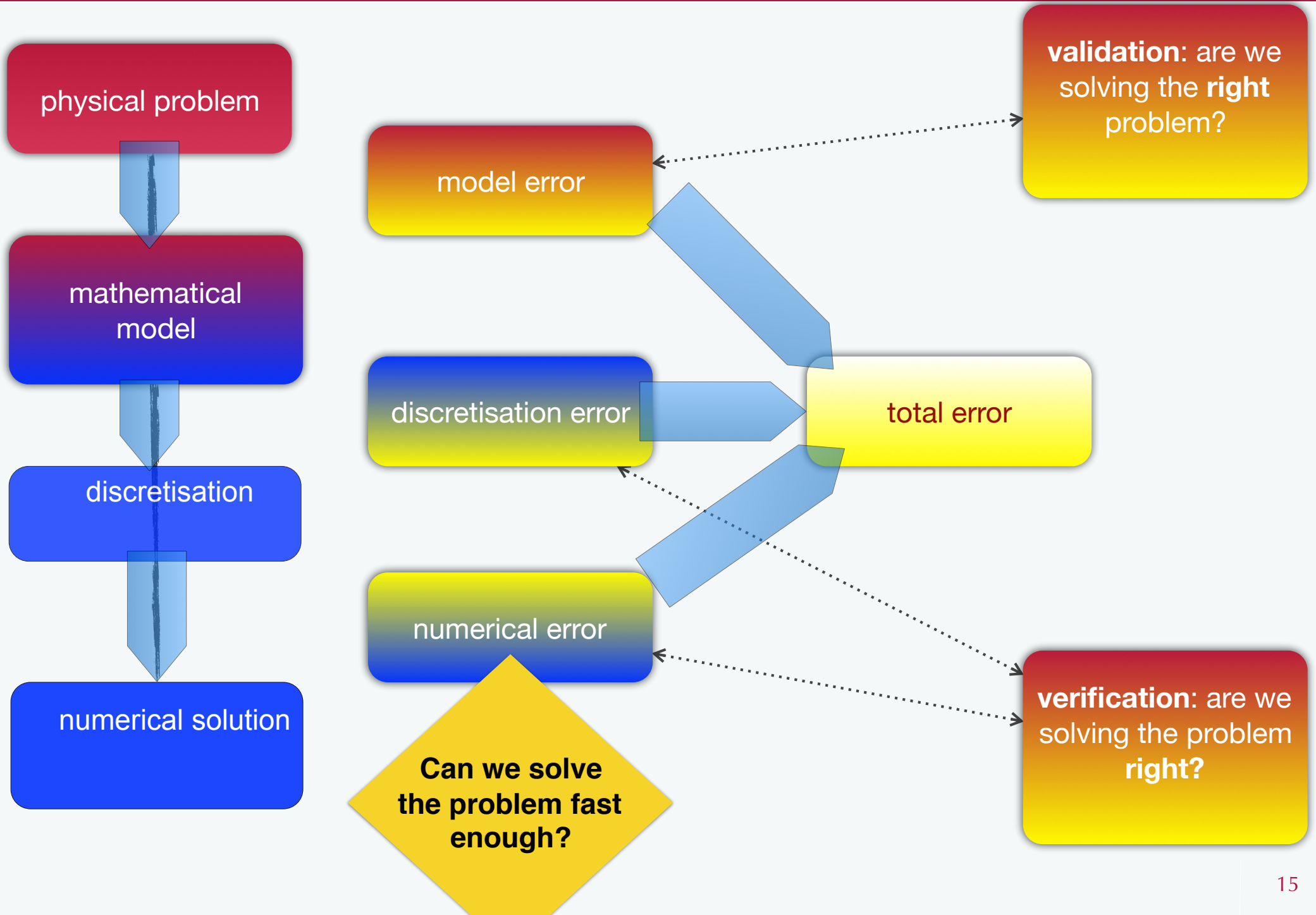
# Modelling and simulation



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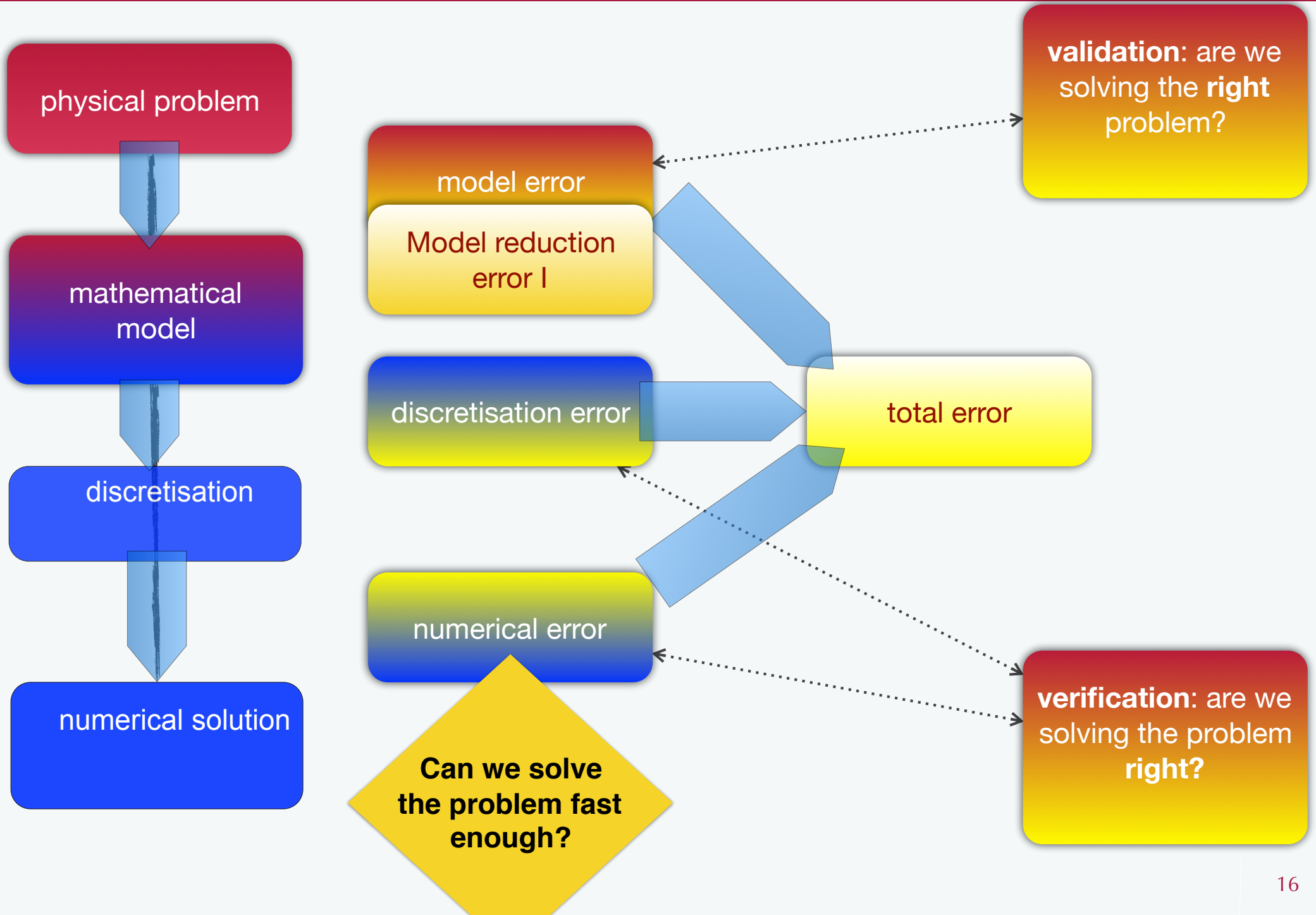


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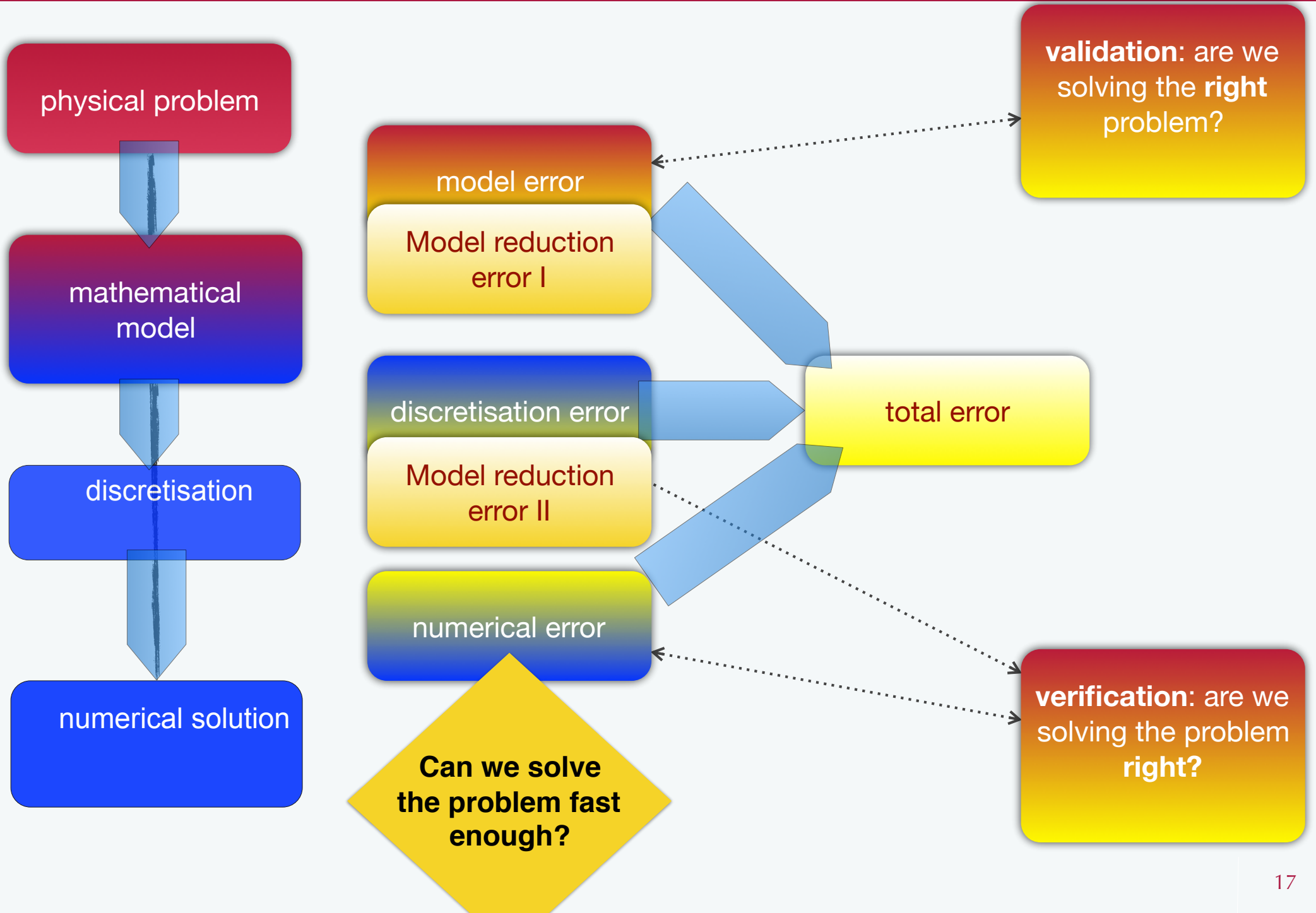




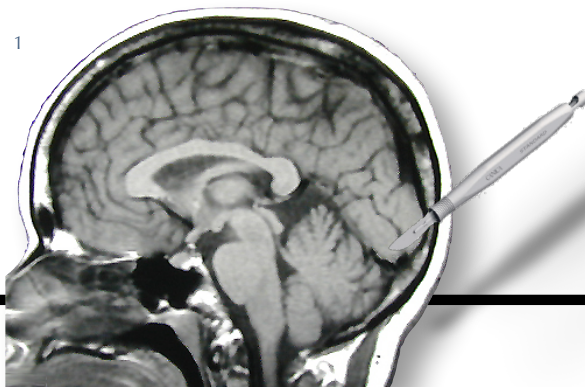
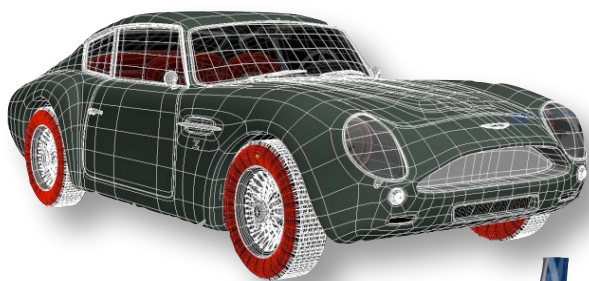
# Modelling and simulation



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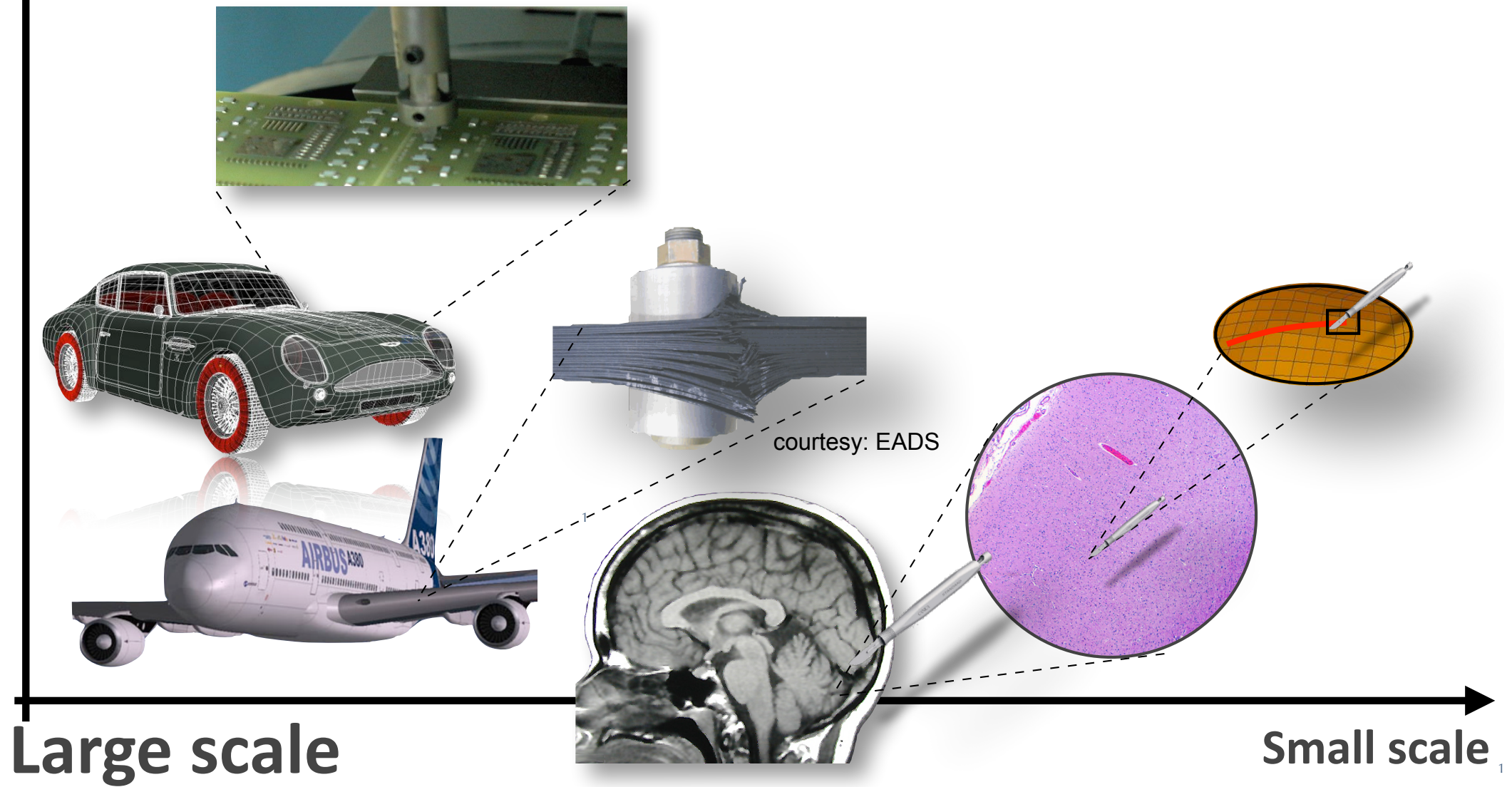
# Discontinuities



Large scale

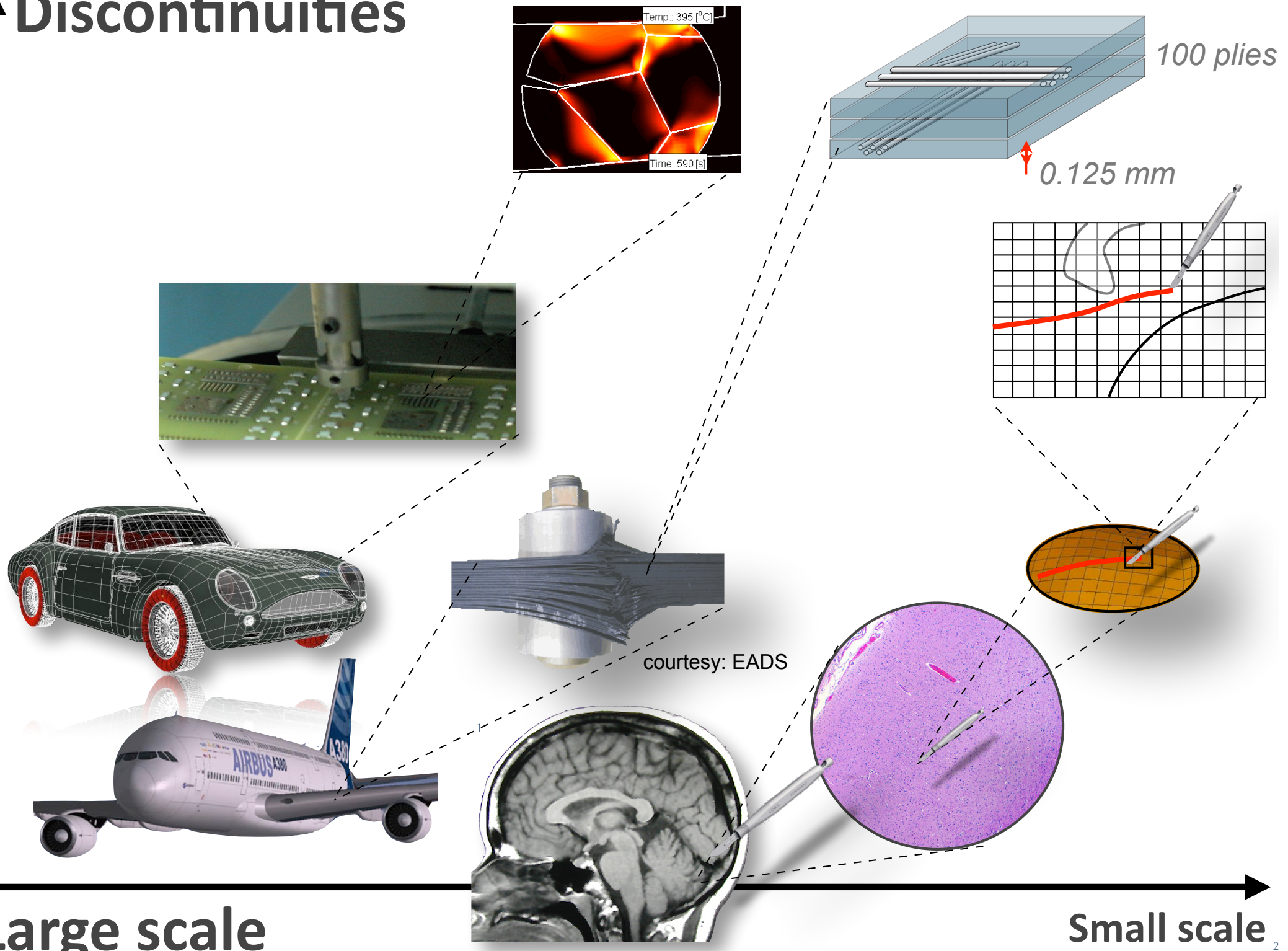
Small scale

# Discontinuities





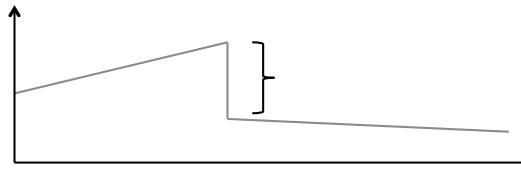
# Discontinuities



# Classification of discontinuities

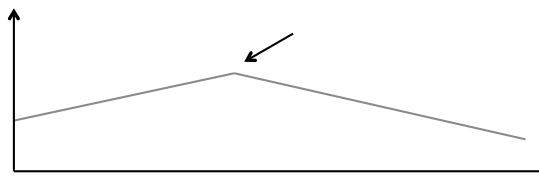
## Strong discontinuities

- The primal field of the solution is discontinuous, e.g. cracks lead to strong discontinuities in the displacement field.



## Weak discontinuities

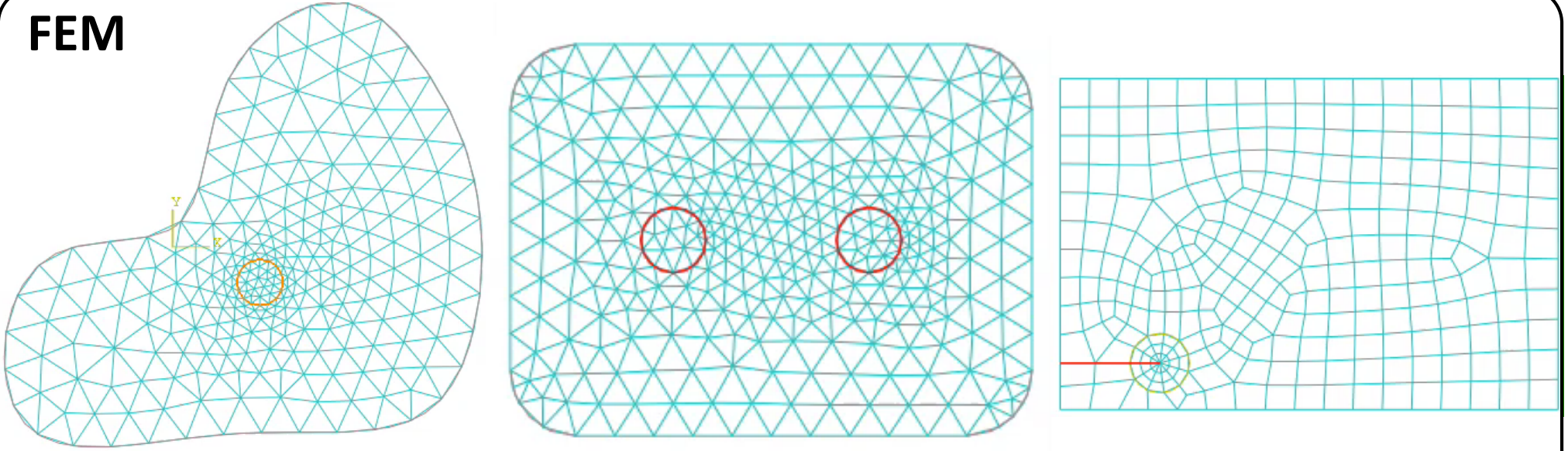
- The first derivative of the solution is discontinuous, e.g. discontinuities in the strain field through a material interface.



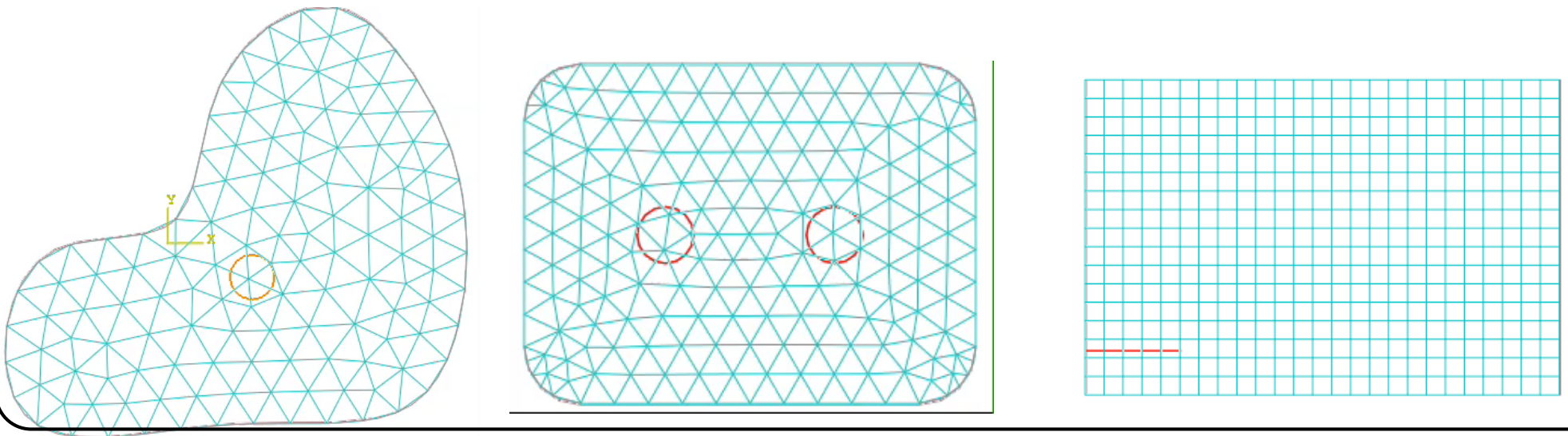




## FEM



## XFEM



# Computational mechanics & computational materials sciences

## Multiscale/field interface problems

### COMPETENCES

#### DISCRETISATION

discrete and continuum approaches

#### MULTI-SCALE FRACTURE

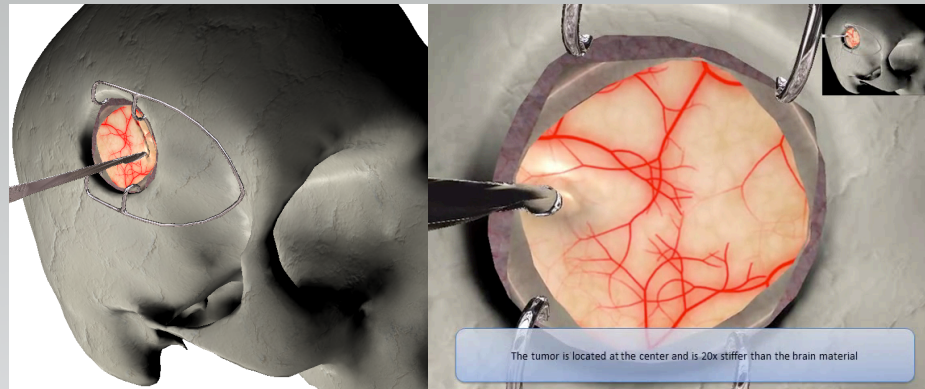
aerospace composites, polycrystalline materials

#### COUPLED PROBLEMS

biofilms, liquid crystals, fluid-structure, batteries

#### QUALITY & ERROR CONTROL

optimise computational time given an accuracy level



*Real-time simulation of cutting during brain surgery*

#### INTERACTIVITY

Reduce computational costs by several orders of magnitude

### APPLICATIONS

#### PERSONALISED MEDICINE

Computer-aided surgery

Computer-aided diagnostics

#### ENGINEERING

Durability & Sustainability

Energy

Aerospace

## Discretization

➡ partition of unity enrichment  
✓ (enriched) meshless methods  
✓ level sets

➡ isogeometric analysis  
➡ implicit boundaries

- ✓ multi-scale & homogenisation
- ✓ algebraic model reduction (using POD)
- ✓ Newton-Krylov, “local/global”, domain decomposition

## Error control

- ✓ XFEM: goal-oriented error estimates
  - ▶ used by CENAERO (Morfeo XFEM)
- ✓ meshless methods for fracture
- ✓ error estimation for reduced models
- ✓ real-time error control



# Model reduction <sup>25</sup>

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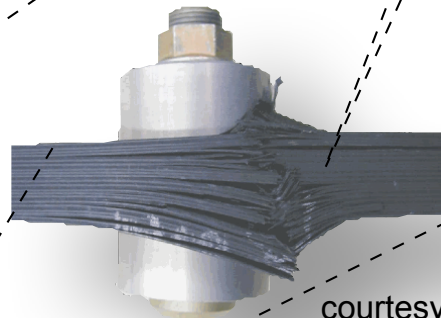
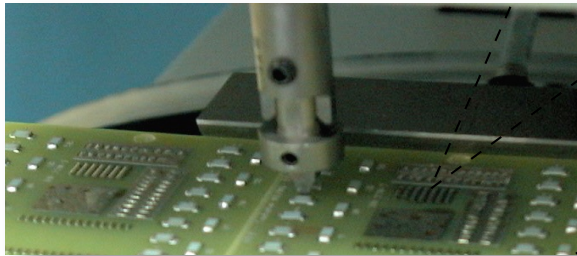
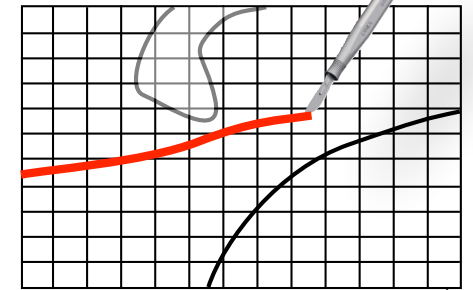
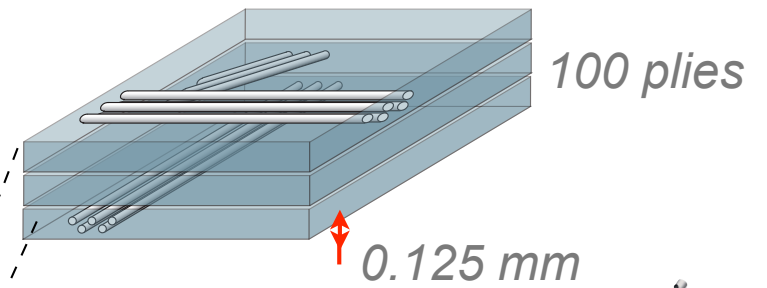
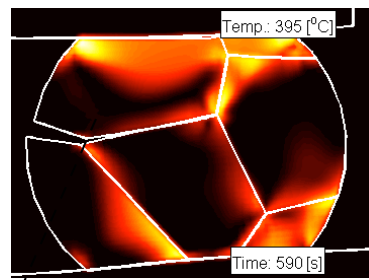
## Discretization

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- ✓ (enriched) meshless methods
- ✓ level sets

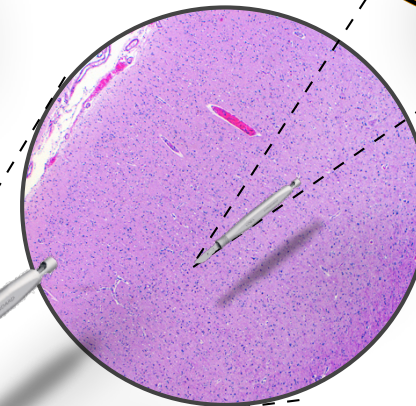
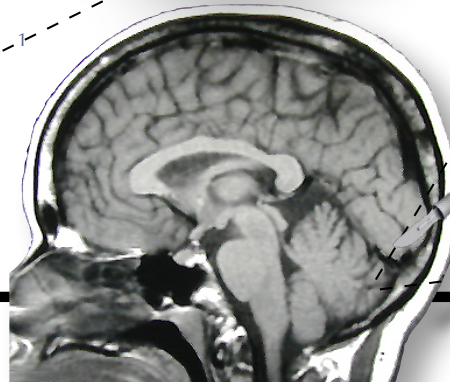
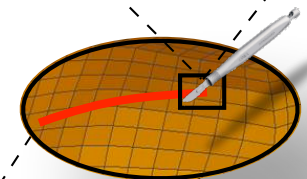
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courtesy: EADS



# Large scale

## Small scale