

# Accessing Power-Law Properties of Post-Seismic Deformation in Land Movements

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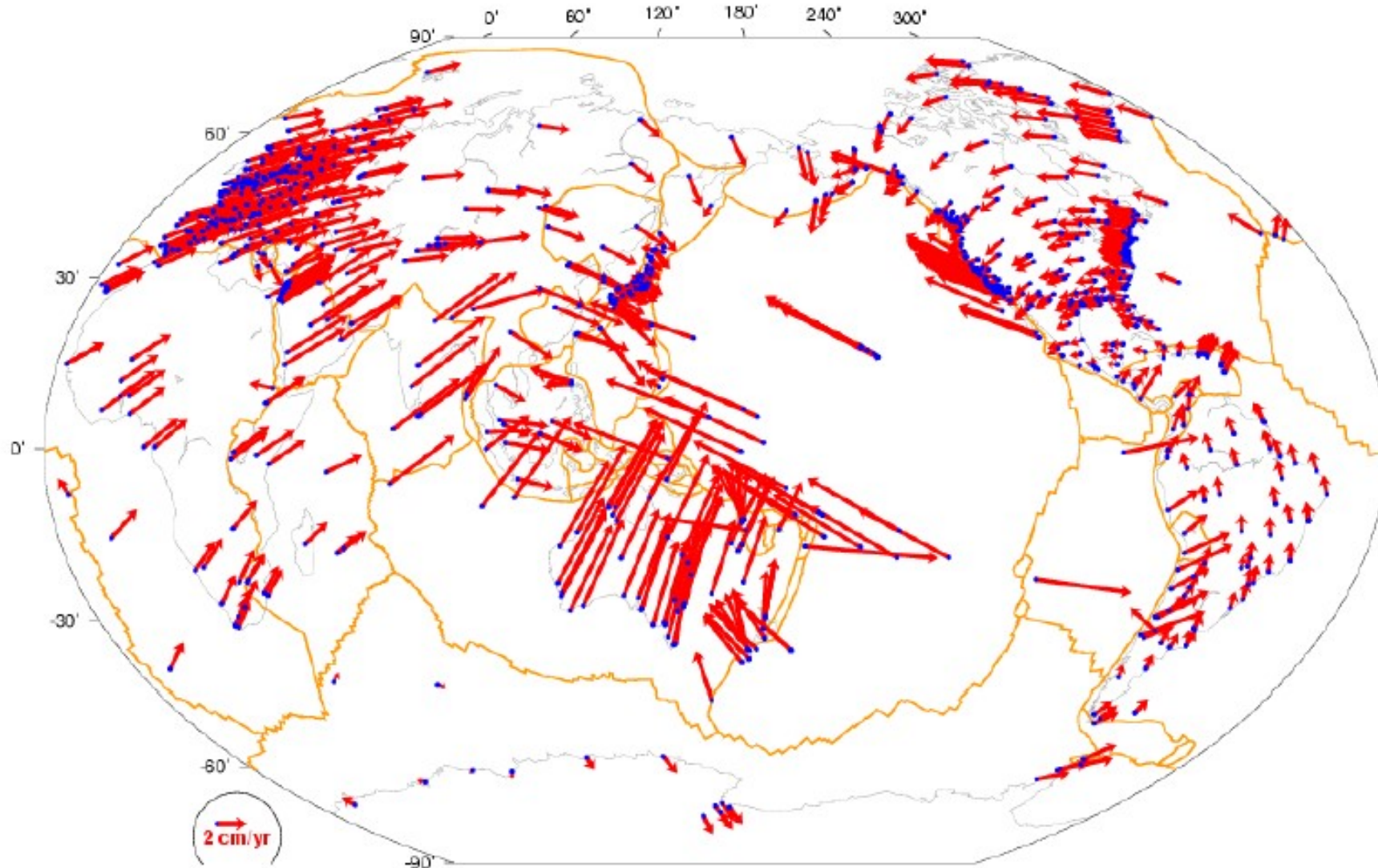
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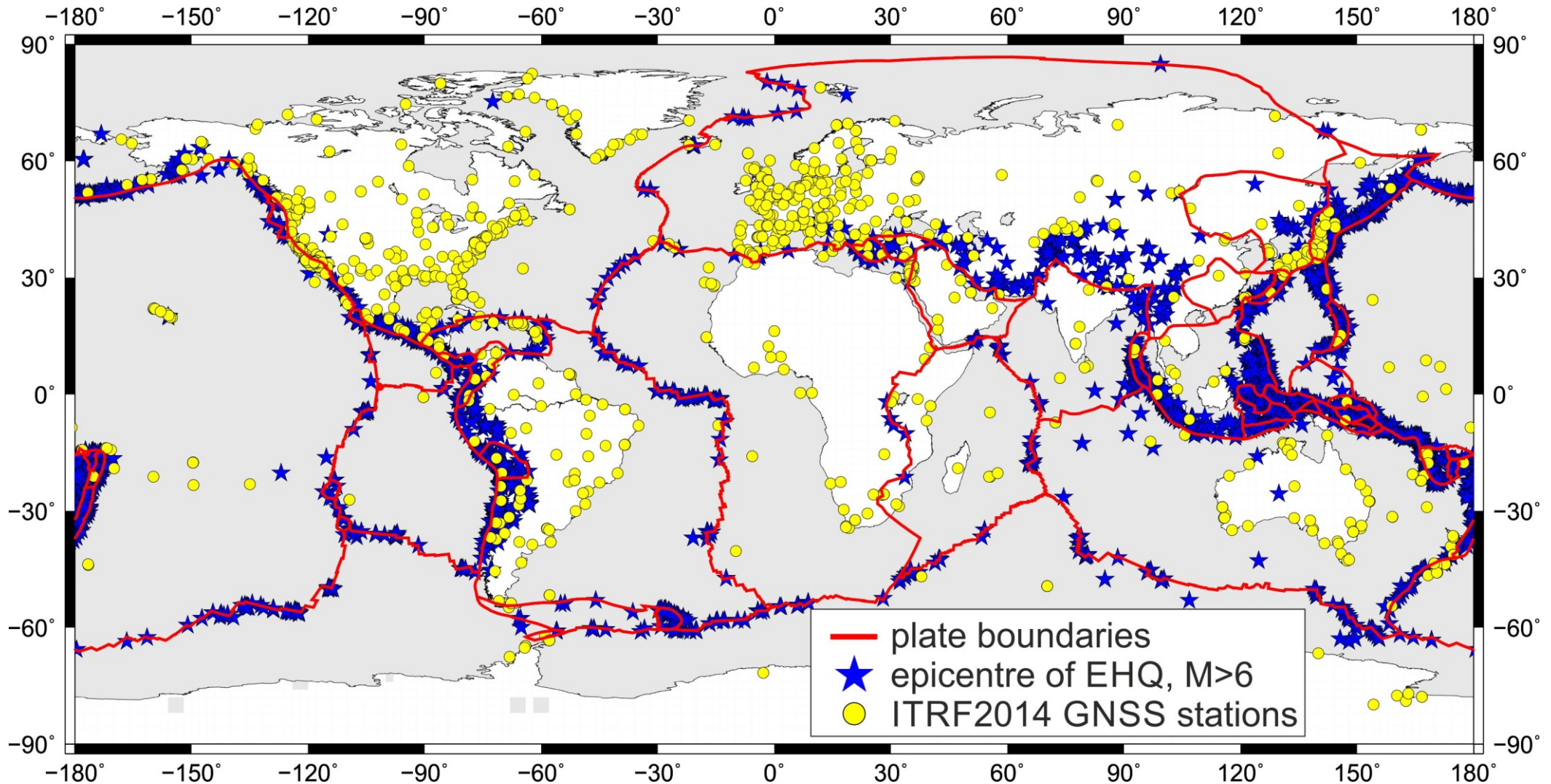


## 1. ITRF2014, GPS velocity field:



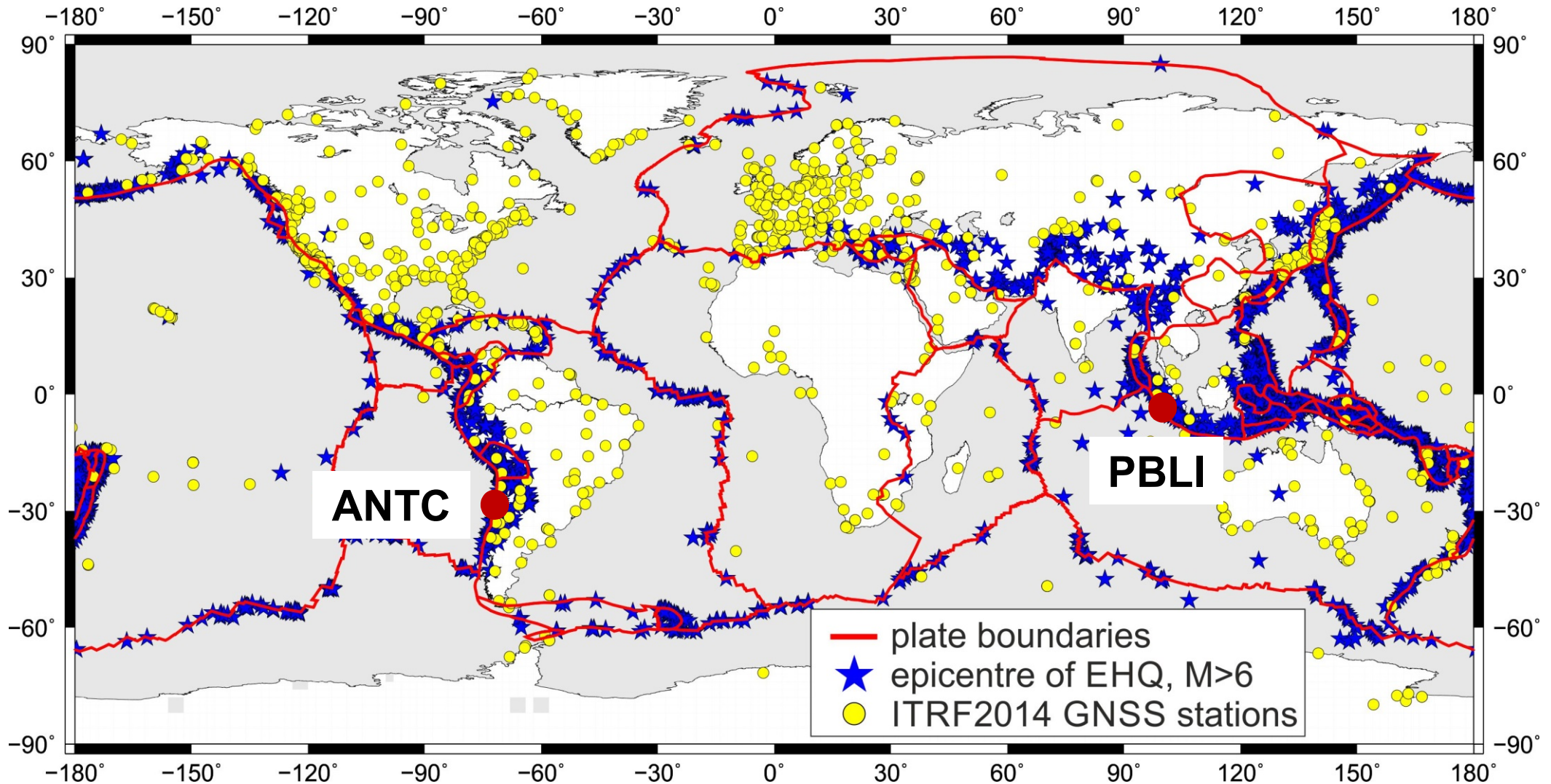
Zuheir Altamimi: „Update on the International Terrestrial Reference Frame (ITRF) and Handling Deformation Caused by Large Earthquakes”. ICG-10, Boulder, USA, 1-6, November, 2015

## 2. Tectonic plates and all EQs since 1995 (3300 events), $M > 6$ :



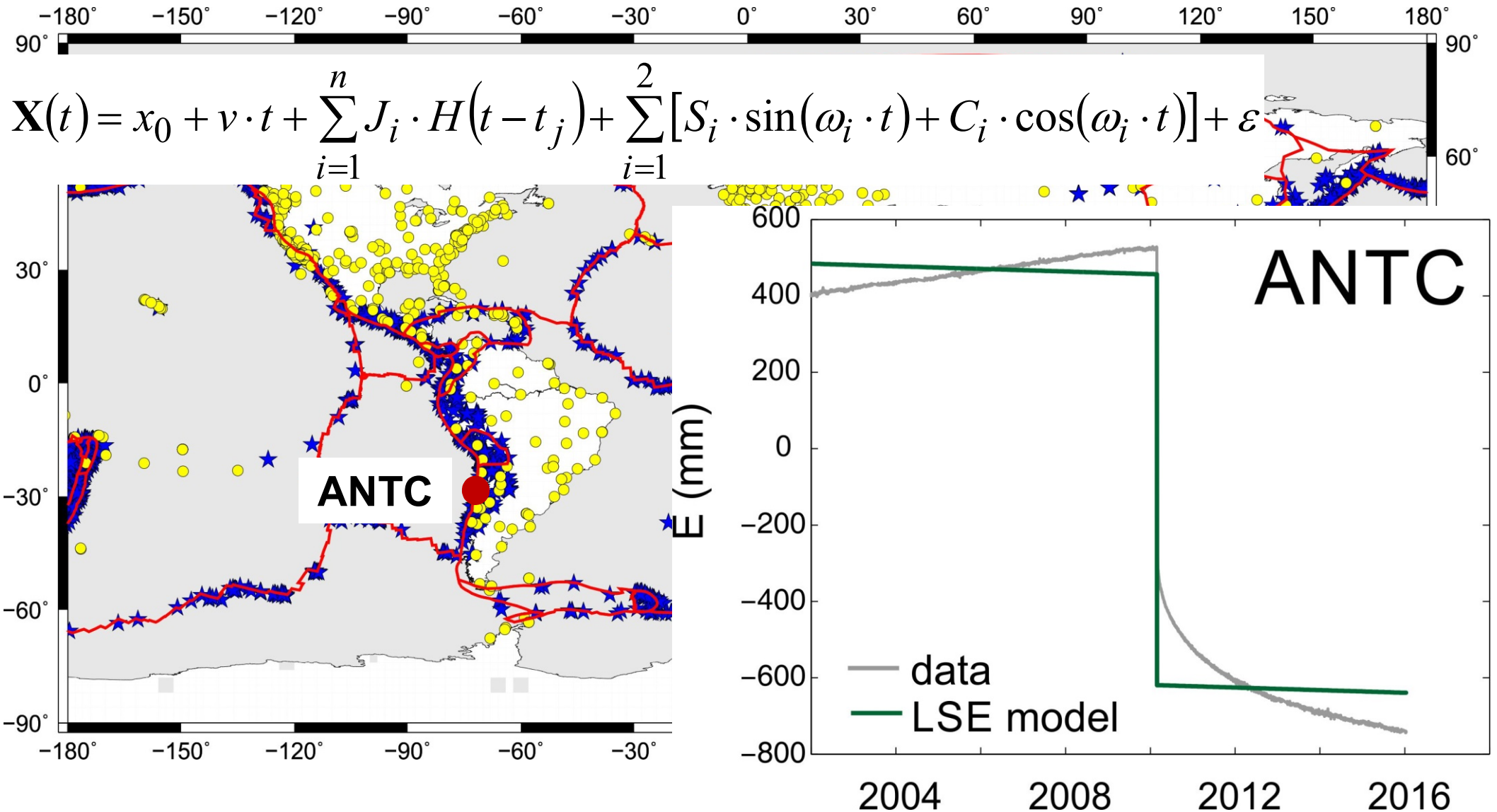
Earthquakes taken from: <http://earthquake.usgs.gov>

### 3. Time series from tectonically active areas:

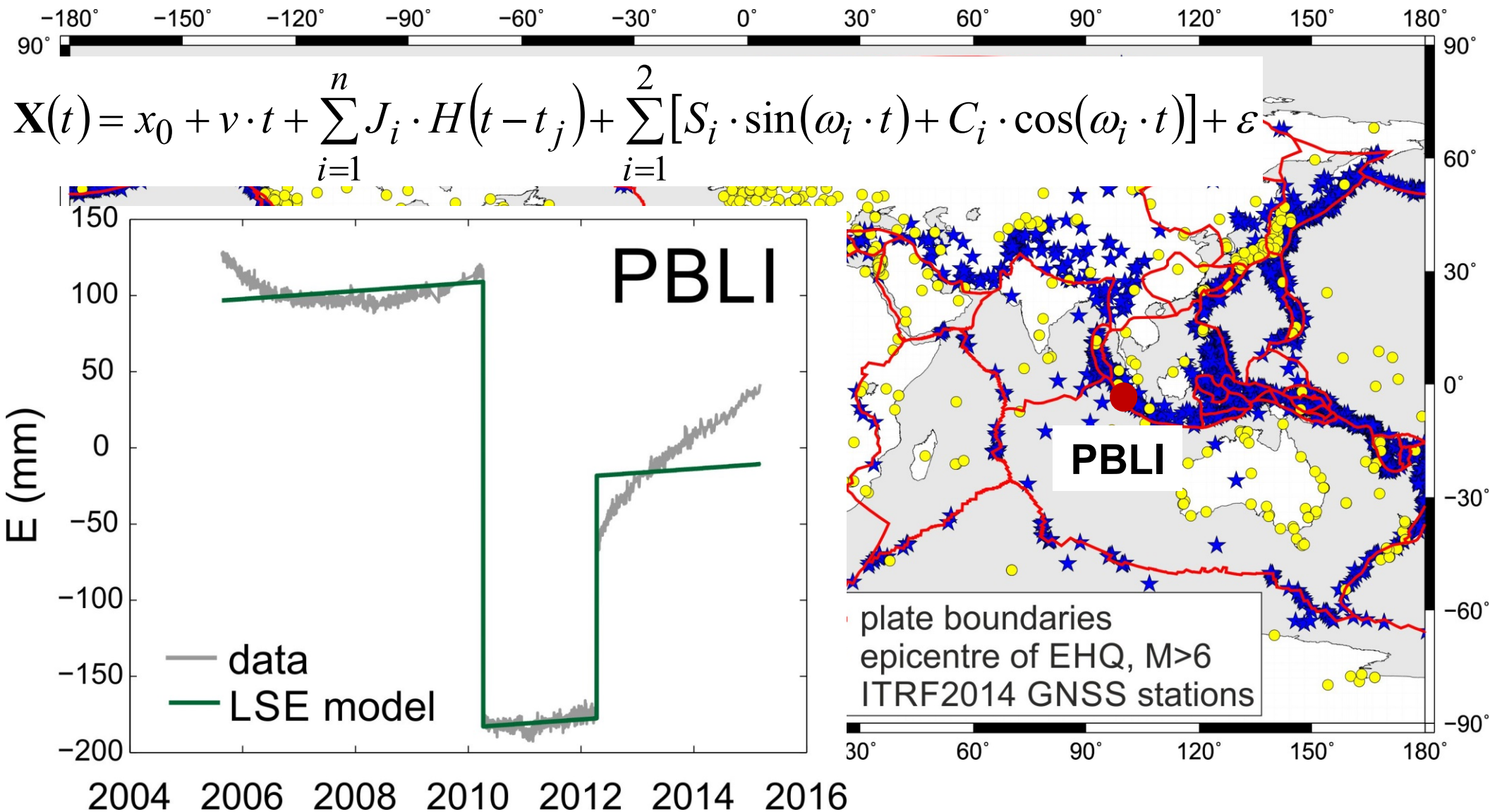


Earthquakes taken from: <http://earthquake.usgs.gov>

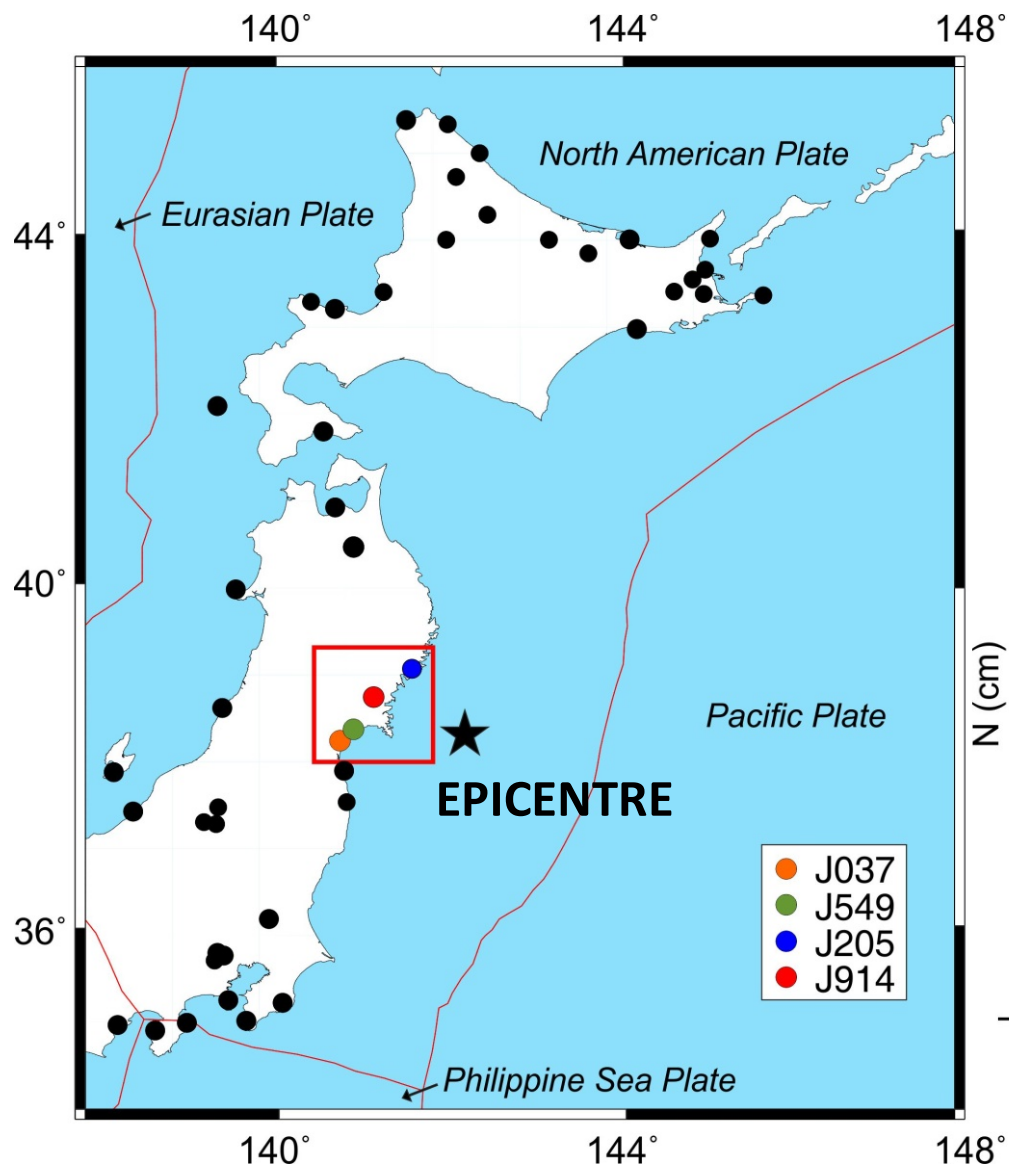
### 3. Time series from tectonically active areas:



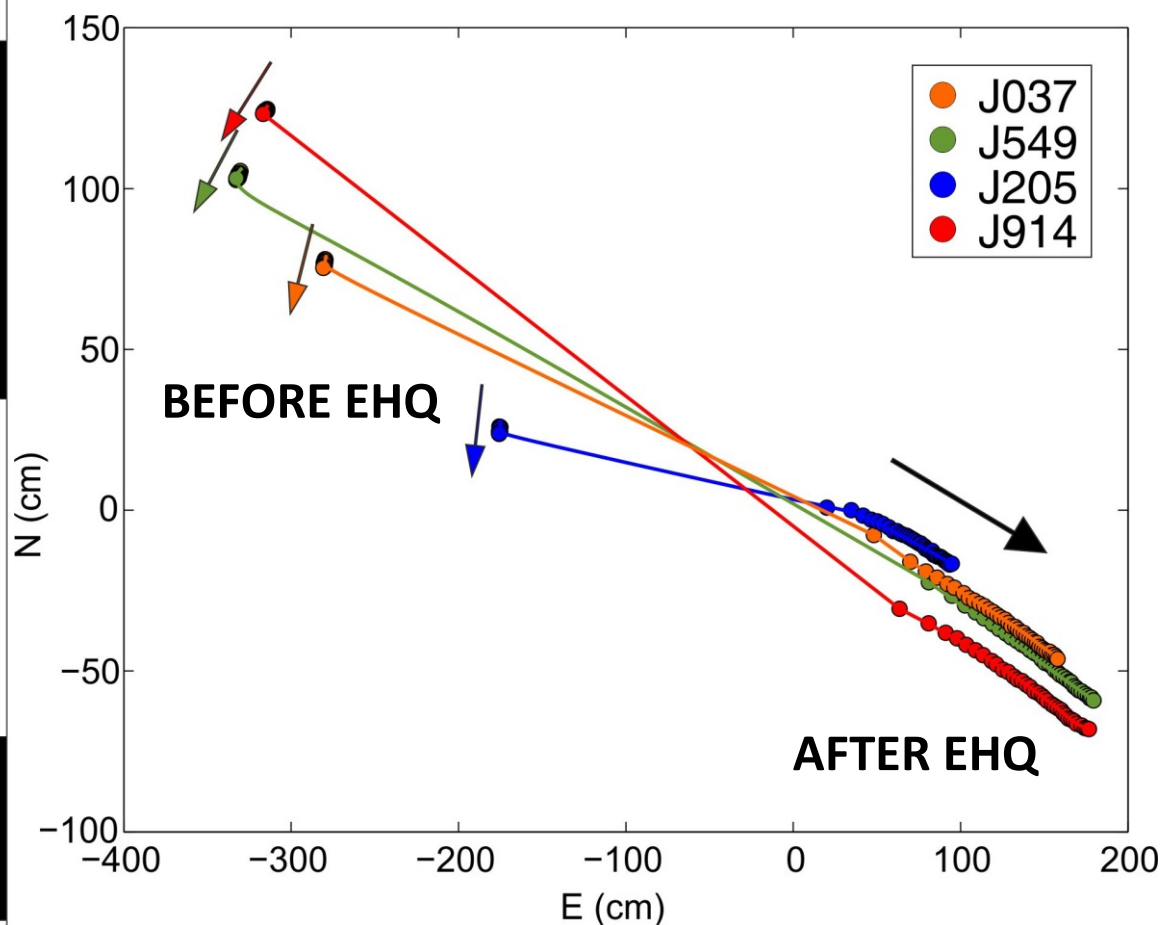
### 3. Time series from tectonically active areas:



### 3. Time series from tectonically active areas:



**Tohoku-Oki earthquake,**  
occurred at 11.03.2011,  $M_L=9.0$  (NEIC)



## 4. How to model a Post-Seismic Deformation (P-SD) (as applied in the ITRF2014)?

- a) exponential,
- b) logarithmic,
- c) exponential + logarithmic
- d) or two exponential

Advantages and drawbacks

functions.

All above need a post-relaxation time ( $e_\tau$  and  $l_\tau$ ).

$$\mathbf{X}(t) = x_0 + v \cdot t + \sum_{i=1}^n J_i \cdot H(t - t_j) + \sum_{i=1}^2 [S_i \cdot \sin(\omega_i \cdot t) + C_i \cdot \cos(\omega_i \cdot t)] +$$
$$+ b \cdot \log\left(1 + \frac{t - t_0}{l_\tau}\right) + c \cdot \left[1 - \exp\left(-\frac{t - t_0}{e_\tau}\right)\right] + \varepsilon$$

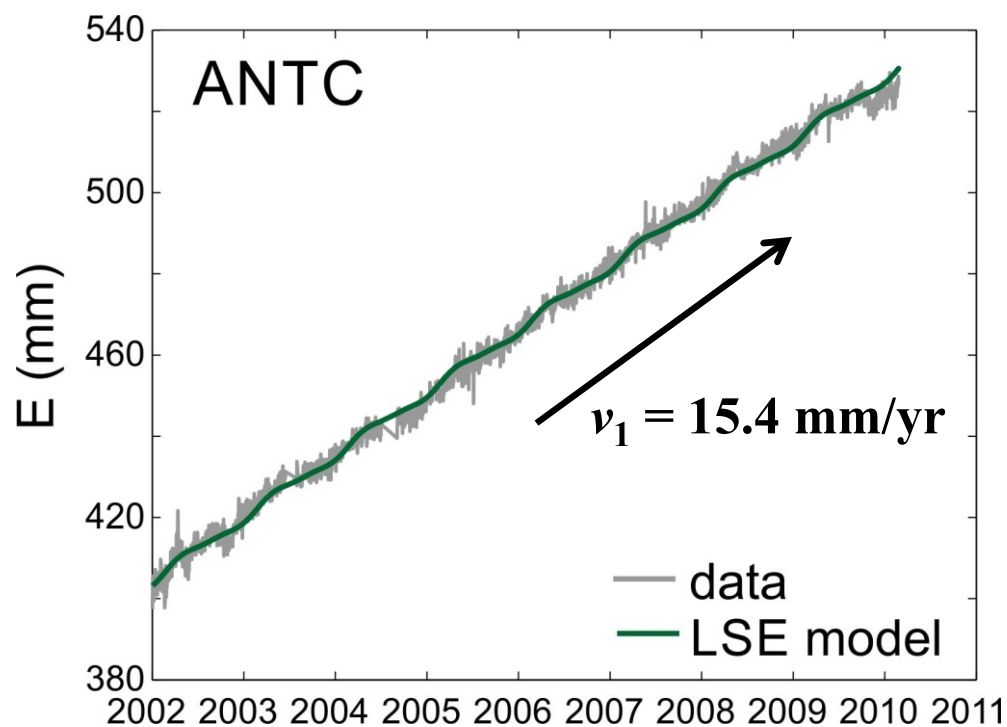
**A misfit between data and model**

**A post-relaxation time**

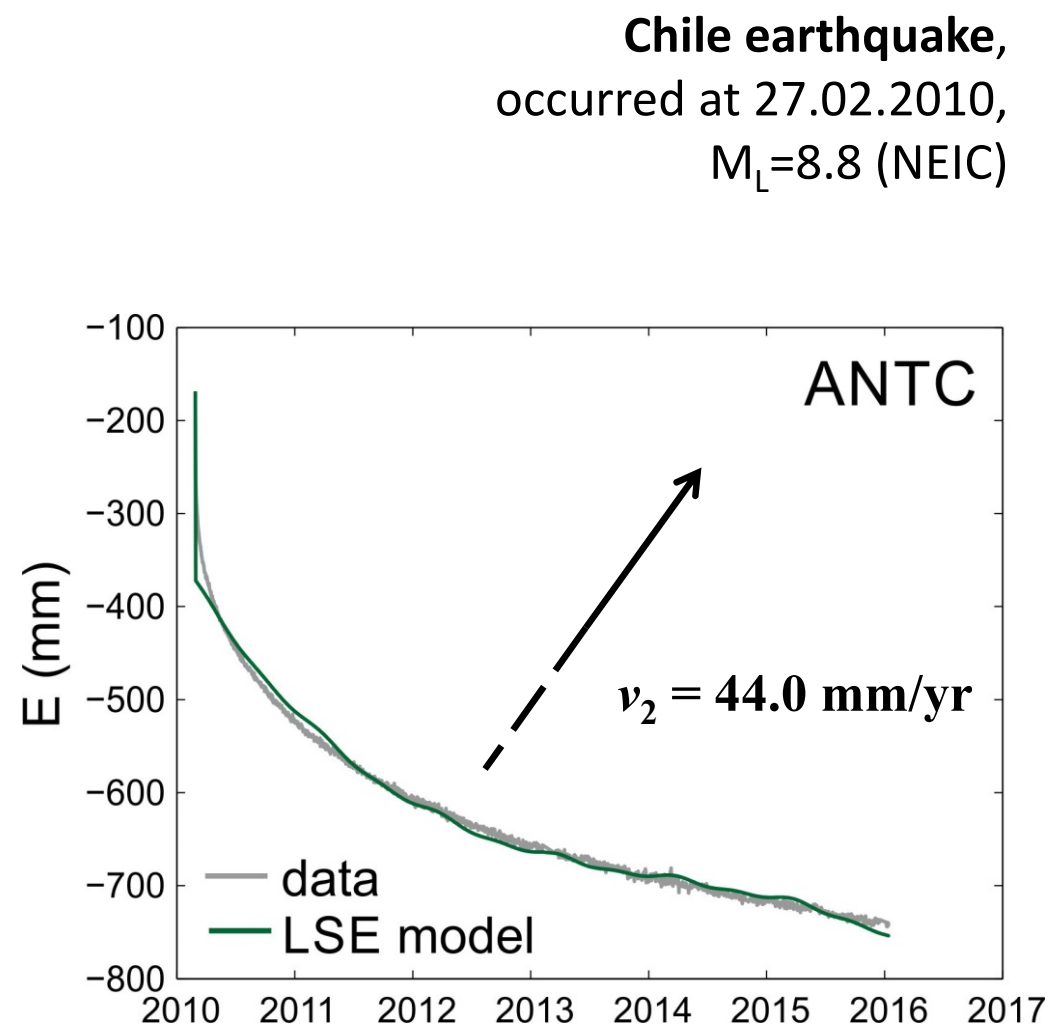


## 4. How to model a Post-Seismic Deformation (P-SD)?

a) cut data into pieces and analyse them separately,

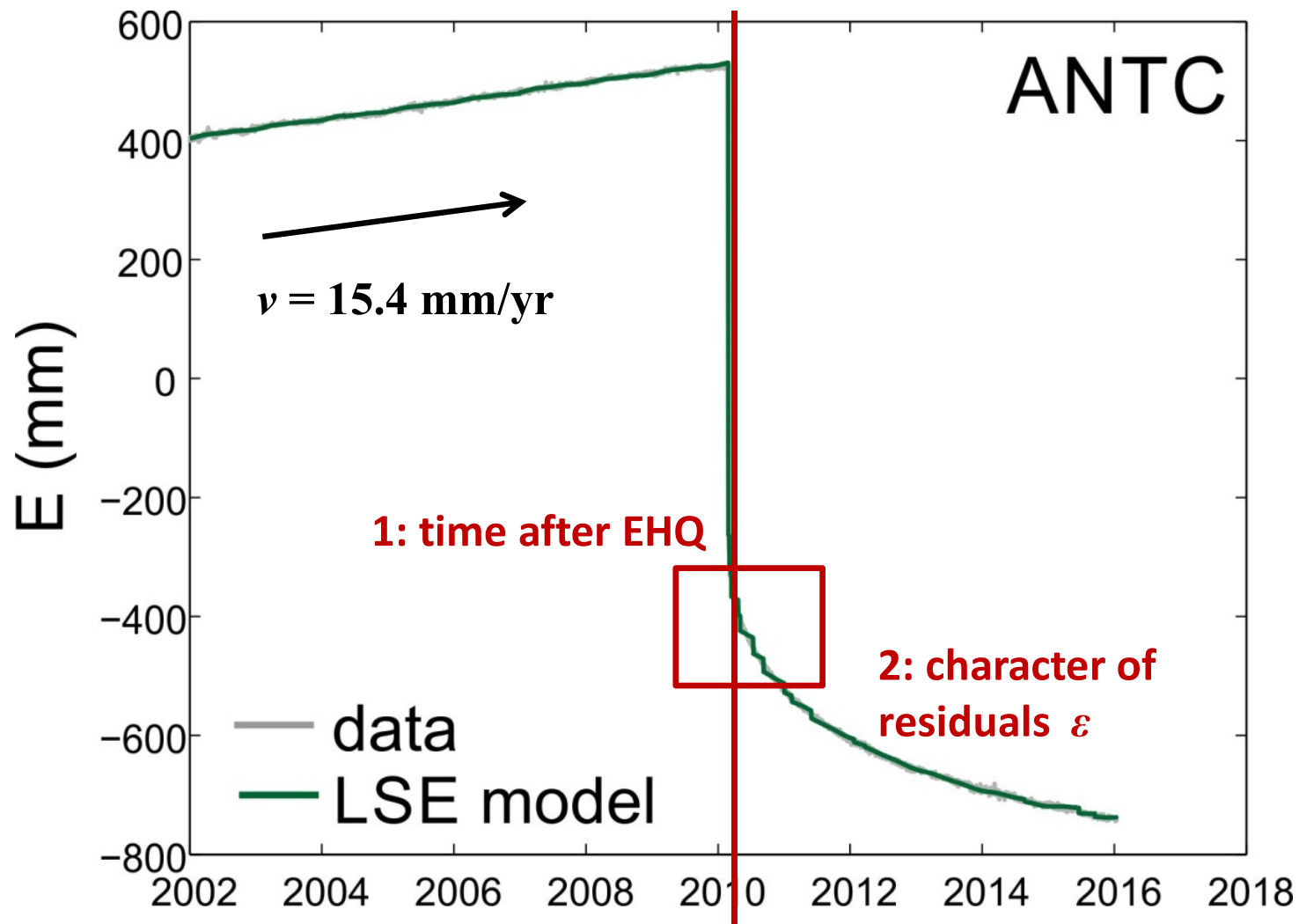


Advantages and drawbacks



## 4. How to model a Post-Seismic Deformation (P-SD)?

b) model entire data,

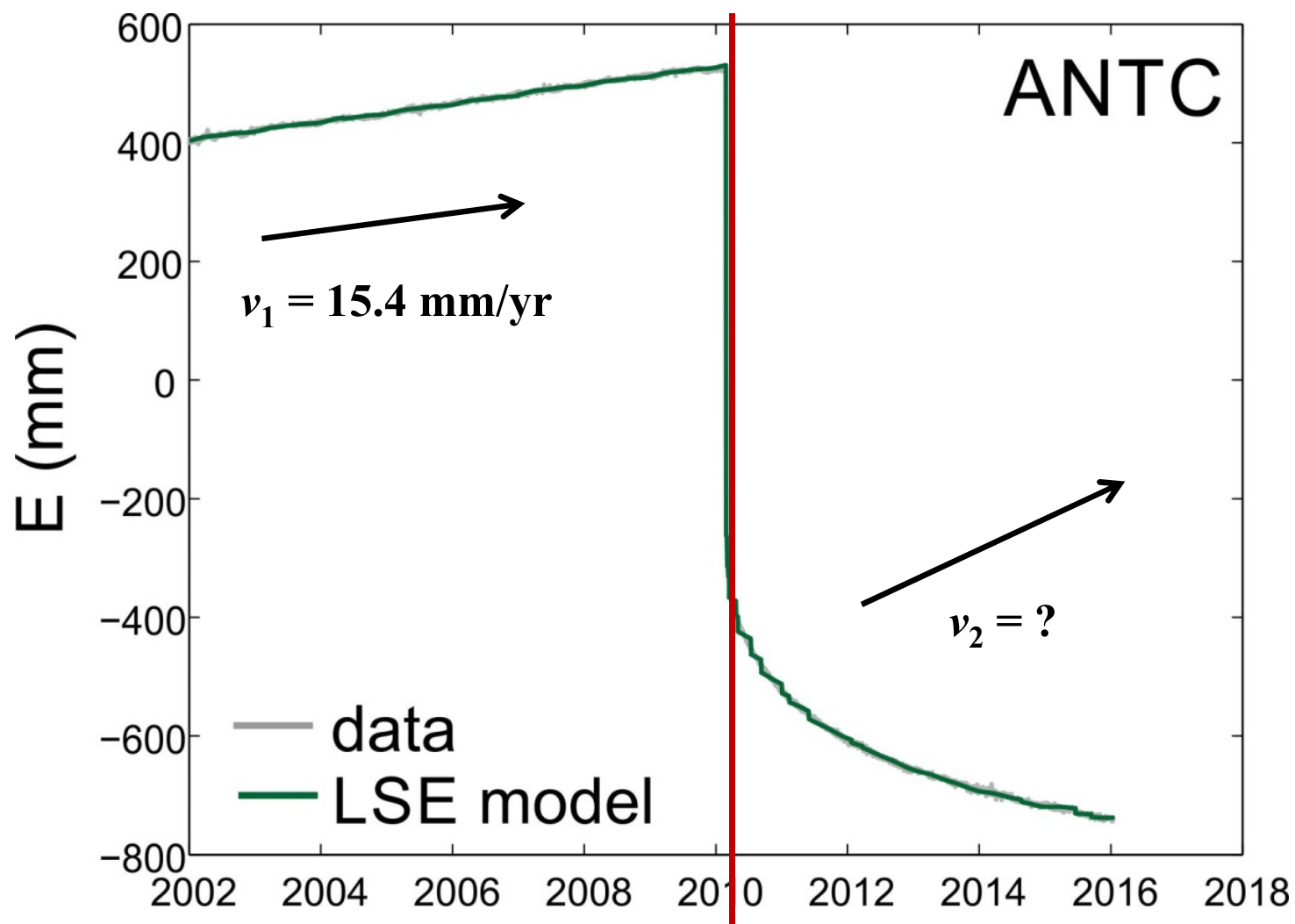


**Chile earthquake,**  
occurred at 27.02.2010,  
 $M_L=8.8$  (NEIC)

Advantages  
and drawbacks

## 4. How to model a Post-Seismic Deformation (P-SD)?

c) apply a multitrend approach.



**Chile earthquake,**  
occurred at 27.02.2010,  
 $M_L=8.8$  (NEIC)

Advantages  
and drawbacks

## 5. Method:

- a) Reformulated Maximum Likelihood Estimation (Bos et al., 2012):

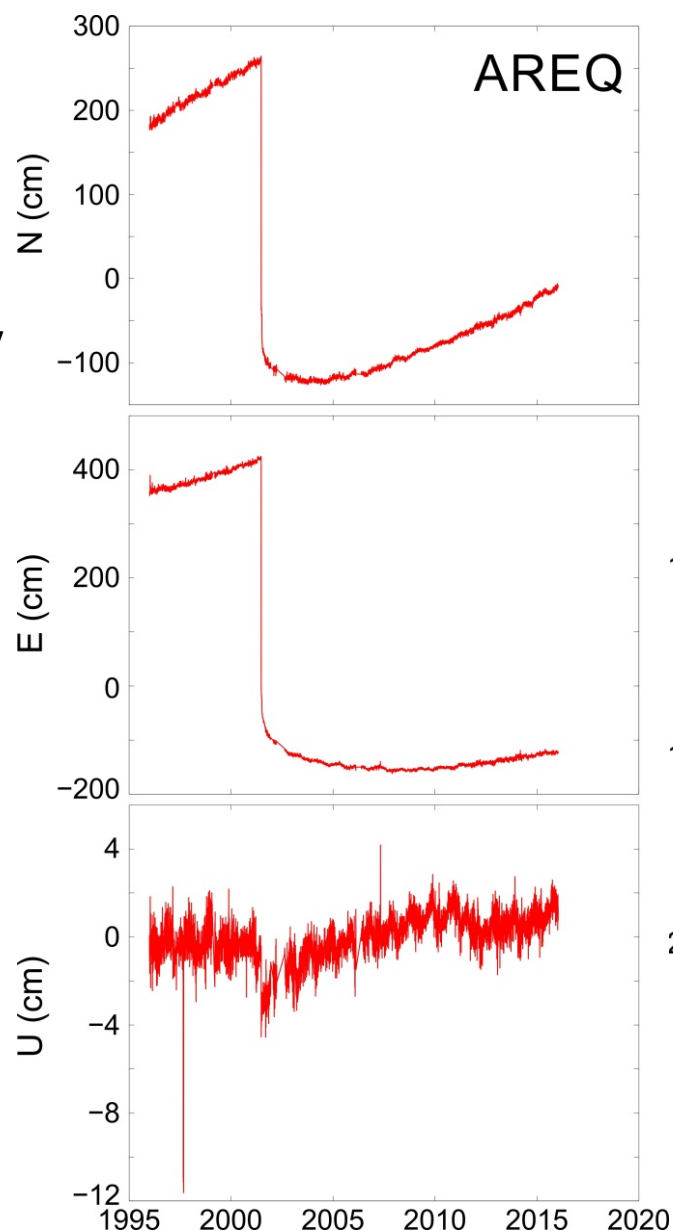
$$\ln[p(\mathbf{r})] = -\frac{1}{2} \left[ (n - m) \ln 2\pi + \ln \det(\check{\mathbf{C}}) + \check{\mathbf{r}}^T \check{\mathbf{C}}^{-1} \check{\mathbf{r}} \right]$$

Assumption of white + power-law noise.

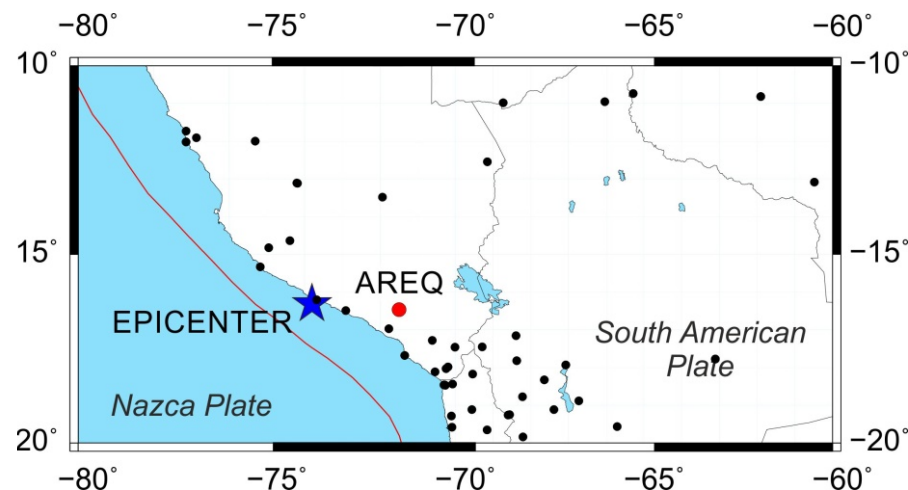
- b) Selection on best model based on Akaike Information Criterion (AIC) and Maximum Likelihood Function (MLF).

## 6. GNSS data:

- Source: NGL, <http://geodesy.unr.edu/> PPP solution,
- Source: TIGA, NS solution,
- Daily samples.



**Peru earthquake,**  
occurred at 23.06.2001,  $M_L=8.4$  (NEIC)



## 6. GNSS data:

a) Cutting into pieces:

**Before EQ (North):**

Noises:

$$\sigma_{PL} = 6.21 \text{ mm/yr}^{-\kappa/4}, \kappa = -0.94$$

Deterministic part:

$$v_1 = 15.10 \pm 0.69 \text{ mm/yr}$$

**Before EQ (East):**

Noises:

$$\sigma_{PL} = 5.88 \text{ mm/yr}^{-\kappa/4}, \kappa = -0.65$$

Deterministic part:

$$v_1 = 11.02 \pm 0.56 \text{ mm/yr}$$

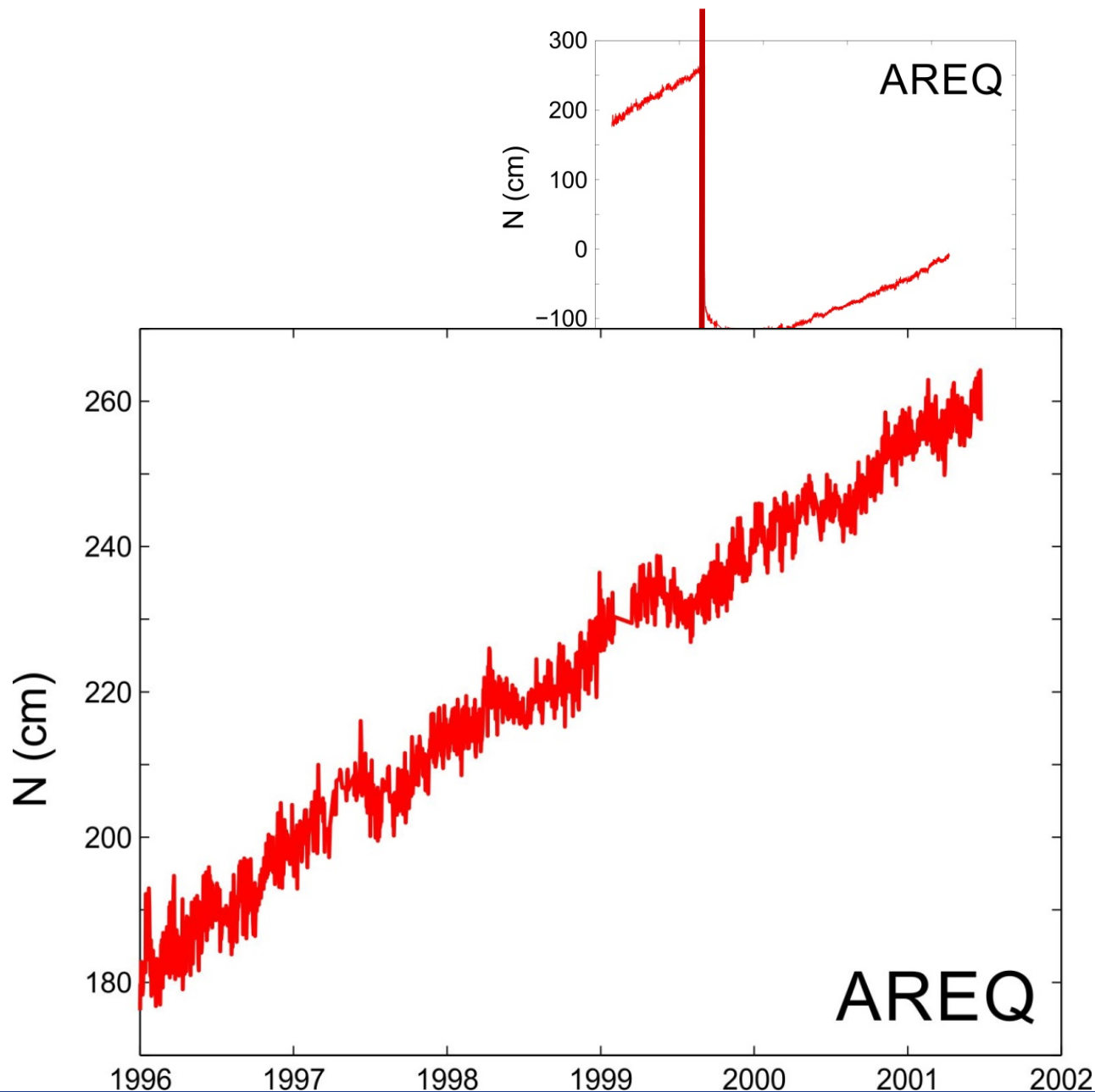
**Before EQ (Up):**

Noises:

$$\sigma_{PL} = 10.39 \text{ mm/yr}^{-\kappa/4}, \kappa = -0.53$$

Deterministic part:

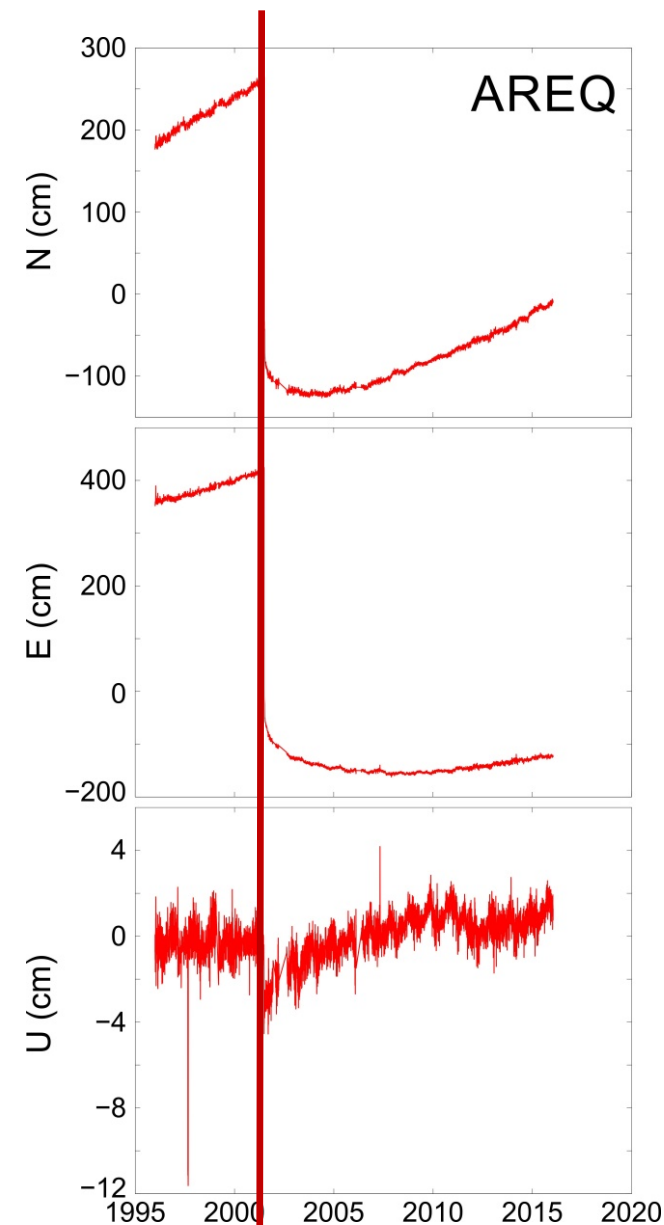
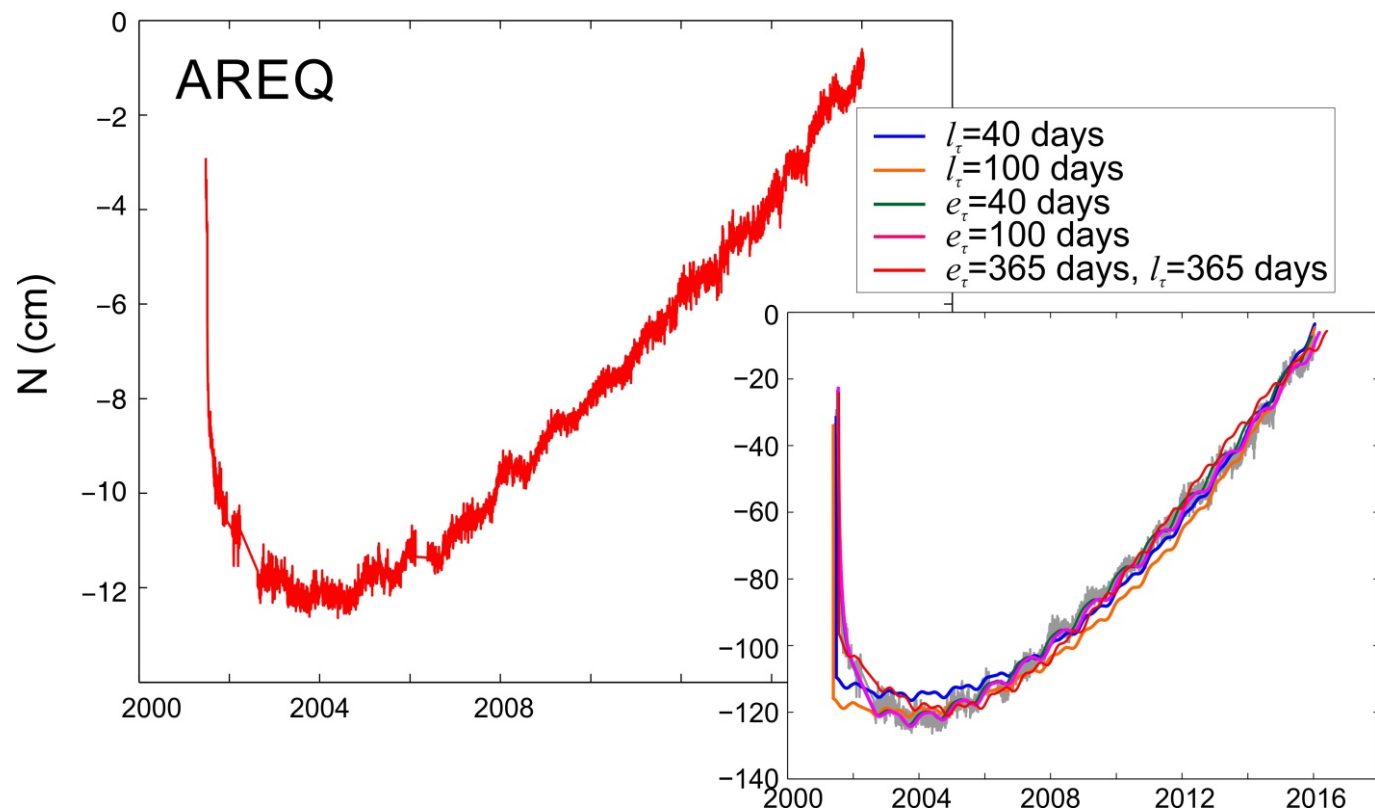
$$v_1 = -1.59 \pm 0.98 \text{ mm/yr}$$



## 6. GNSS data:

### a) Cutting into pieces (after EQ):

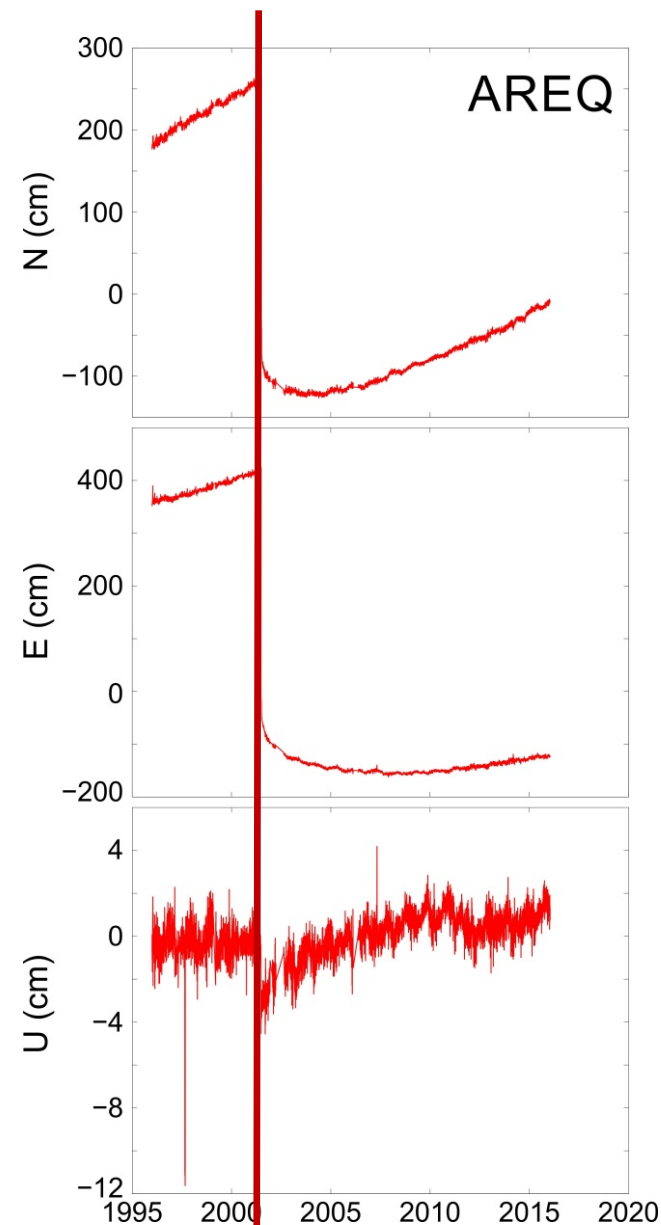
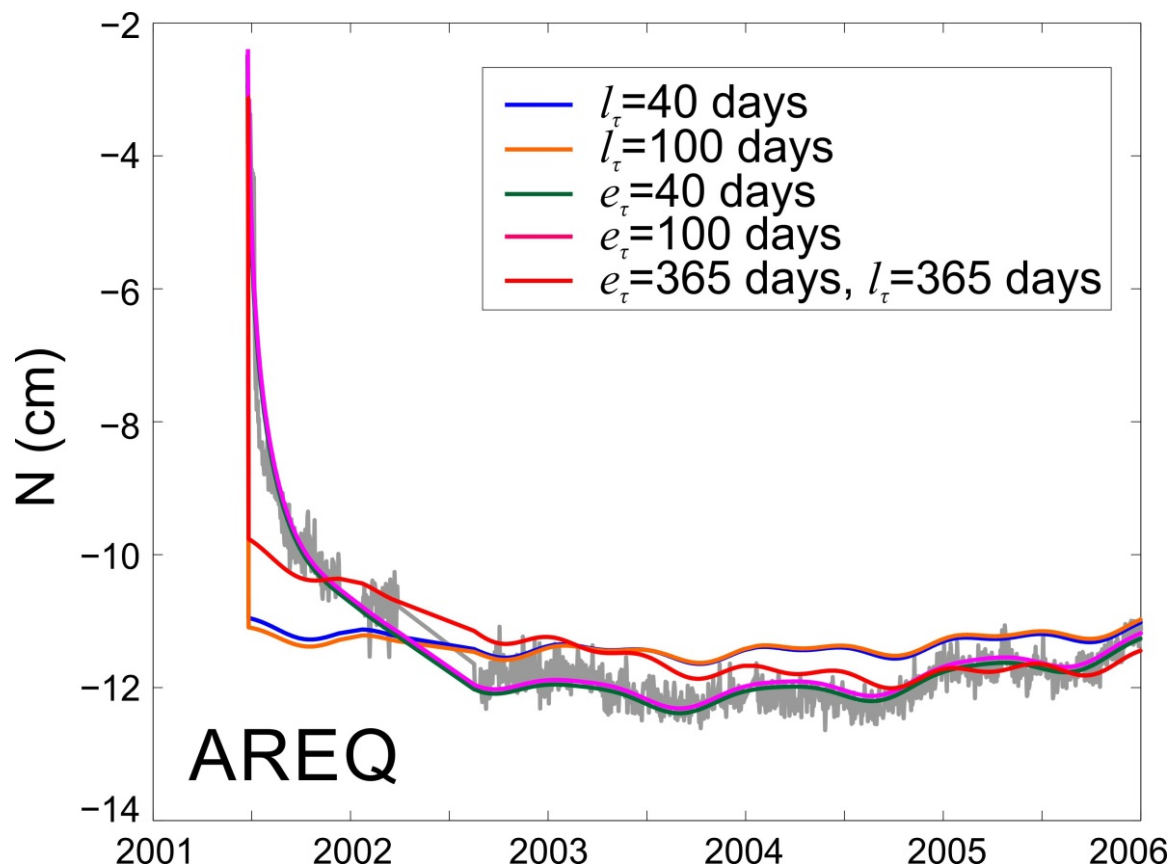
Post-relaxation time ( $e_\tau$  and  $l_\tau$  in days) is a main issue.



## 6. GNSS data:

### a) Cutting into pieces (after EQ):

Post-relaxation time ( $e_\tau$  and  $l_\tau$  in days) is a main issue,  
AIC and MLF differs a lot (of even 550).





## 6. GNSS data:

### a) Cutting into pieces (after EHQ):

Post-relaxation time ( $e_\tau$  and  $l_\tau$  in days) is a main issue,

AIC and MLF differs a lot (of even 550).

#### BEFORE EHQ (North):

Noises:

$$\sigma_{PL} = 6.21 \text{ mm/yr}^{-\kappa/4}, \kappa = -0.94$$

Deterministic part:

$$v_1 = 15.10 \pm 0.69 \text{ mm/yr}$$

#### AFTER EHQ (North):

$$e_\tau = 1, l_\tau = 811$$

(lowest AIC & greatest MLF)

Noises:

$$\sigma_{PL} = 4.04 \text{ mm/yr}^{-\kappa/4}, \kappa = -0.93$$

Deterministic part:

$$v_2 = 18.49 \pm 0.59 \text{ mm/yr}$$

#### BEFORE EHQ (East):

Noises:

$$\sigma_{PL} = 5.88 \text{ mm/yr}^{-\kappa/4}, \kappa = -0.65$$

Deterministic part:

$$v_1 = 11.02 \pm 0.56 \text{ mm/yr}$$

#### AFTER EHQ (East):

$$e_\tau = 1, l_\tau = 871$$

(lowest AIC & greatest MLF)

Noises:

$$\sigma_{PL} = 4.69 \text{ mm/yr}^{-\kappa/4}, \kappa = -1.05$$

Deterministic part:

$$v_2 = 14.73 \pm 0.76 \text{ mm/yr}$$

#### BEFORE EHQ (Up):

Noises:

$$\sigma_{PL} = 10.39 \text{ mm/yr}^{-\kappa/4}, \kappa = -0.53$$

Deterministic part:

$$v_1 = -1.59 \pm 0.98 \text{ mm/yr}$$

#### AFTER EHQ (Up):

$$e_\tau = 121, l_\tau = 1$$

(lowest AIC & greatest MLF)

Noises:

$$\sigma_{PL} = 9.92 \text{ mm/yr}^{-\kappa/4}, \kappa = -0.71$$

Deterministic part:

$$v_2 = 1.31 \pm 0.83 \text{ mm/yr}$$

## 6. GNSS data:

### b) model entire data:

Post-relaxation time ( $e_\tau$  and  $l_\tau$  in days) is a main issue.

#### Entire data (East):

$$e_\tau = 1, l_\tau = 781$$

(lowest AIC & greatest MLF)

Noises:

$$\sigma_{PL} = 5.09 \text{ mm/yr}^{-\kappa/4}, \kappa = -1.25$$

Deterministic part:

$$v = 12.25 \pm 0.53 \text{ mm/yr}$$

#### After EQ (East):

$$e_\tau = 1, l_\tau = 871$$

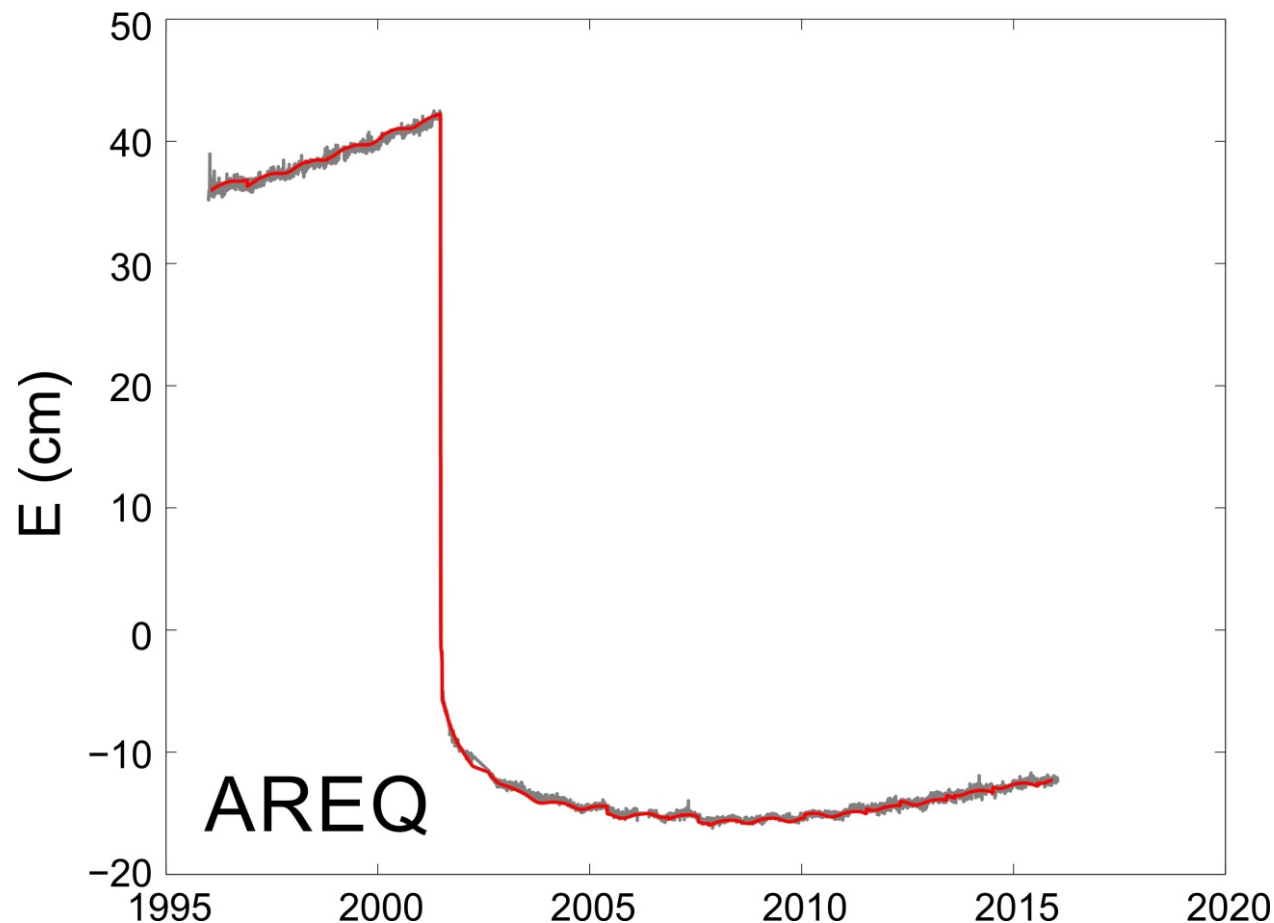
(lowest AIC & greatest MLF)

Noises:

$$\sigma_{PL} = 4.70 \text{ mm/yr}^{-\kappa/4}, \kappa = -1.05$$

Deterministic part:

$$v = 14.72 \pm 0.76 \text{ mm/yr}$$



## 7. Conclusions:

- a) Velocity of GNSS station changes after earthquake.
- b) The post-seismic decay has to be modelled to properly analyse noises.
- c) Few different approaches can be applied to time series affected by earthquakes.
- d) The spectral index of power-law dependencies goes towards flicker noise.

# THANK YOU FOR ATTENTION

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Maps were drawn in the Generic Mapping Tools (Wessel et al., 2013).

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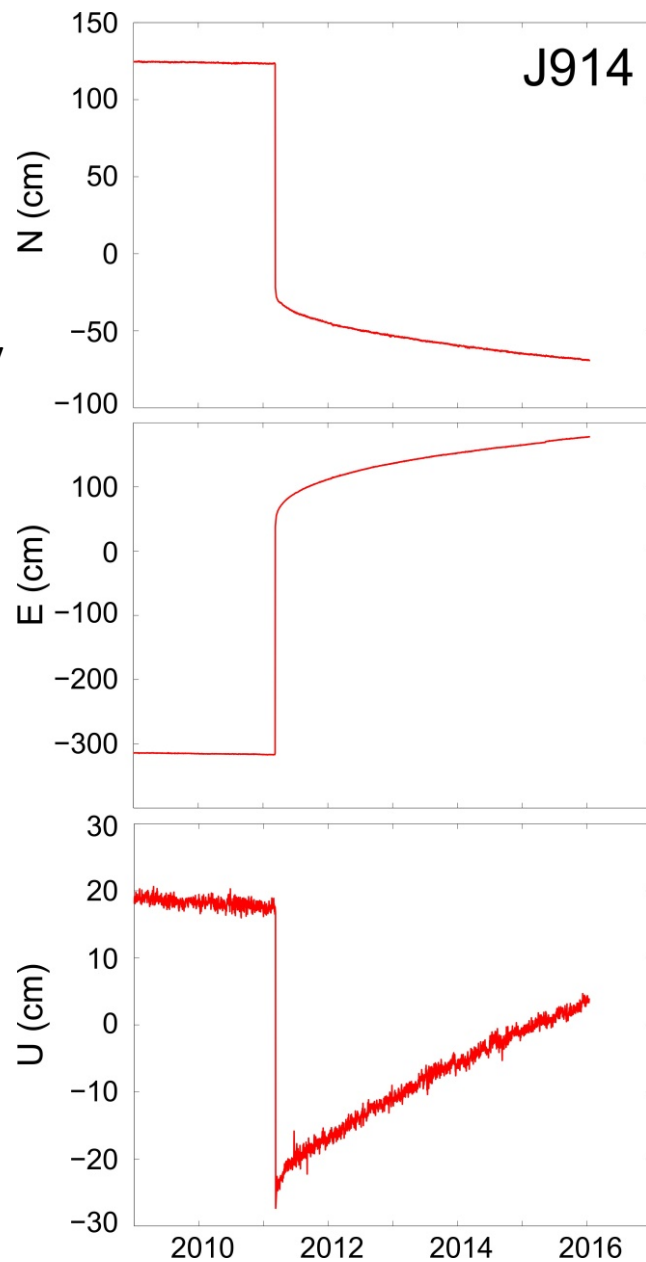
**Addisu Hunegnaw** is financed by the University of Luxembourg projects SGSL & GSCG.

**Machiel Simon Bos** is financially supported by Portuguese funds through FCT in the scope of the Project IDL-FCT-UID/GEO/50019/2013 and grant number SFRH/BPD/89923/2012.

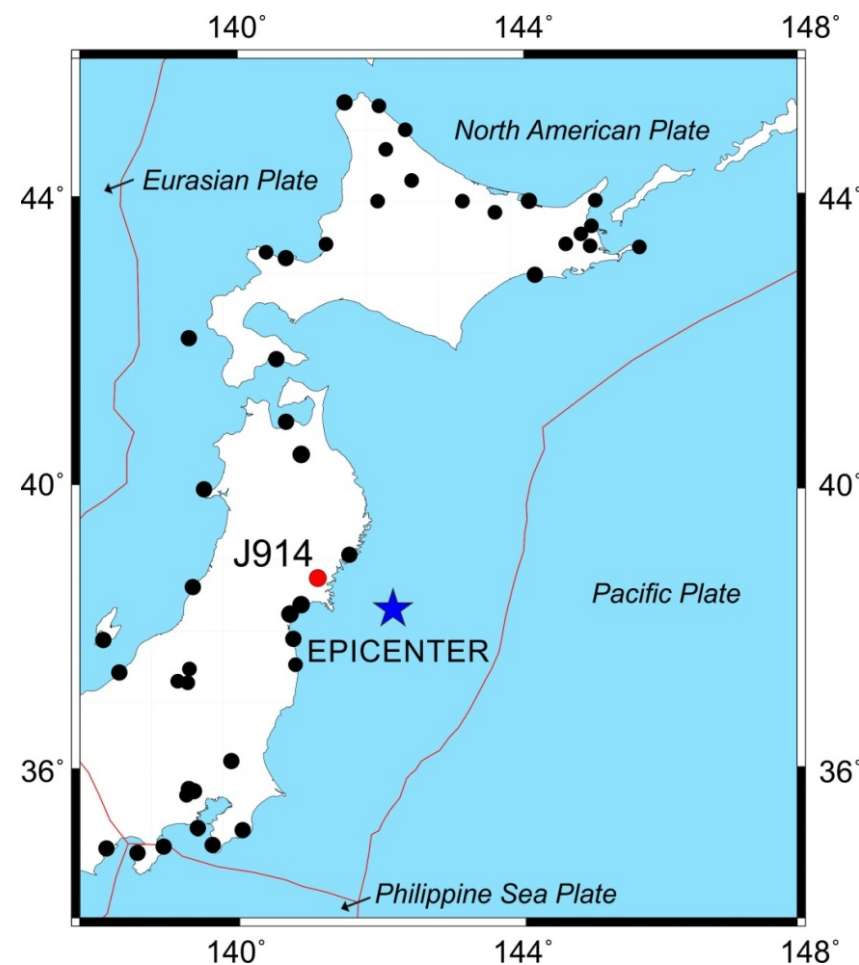
**Machiel Bos and Rui Fernandes** are members of the project FCT UID/GEO/50019/2013 - Instituto Dom Luiz.

## 6. GNSS data:

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- Source: TIGA, NS solution,
- Daily samples.



**Tohoku-Oki earthquake,**  
occurred at 11.03.2011,  $M_L=9.0$  (NEIC)



## 6. GNSS data:

a) Cutting into pieces (before EQ):

### North:

Noises:

$$\sigma_{PL} = 2.73 \text{ mm/yr}^{-\kappa/4}, \kappa = -0.36$$

Deterministic part:

$$v_1 = -6.20 \pm 0.72 \text{ mm/yr}$$

### East:

Noises:

$$\sigma_{PL} = 3.01 \text{ mm/yr}^{-\kappa/4}, \kappa = -0.36$$

Deterministic part:

$$v_1 = -14.31 \pm 0.79 \text{ mm/yr}$$

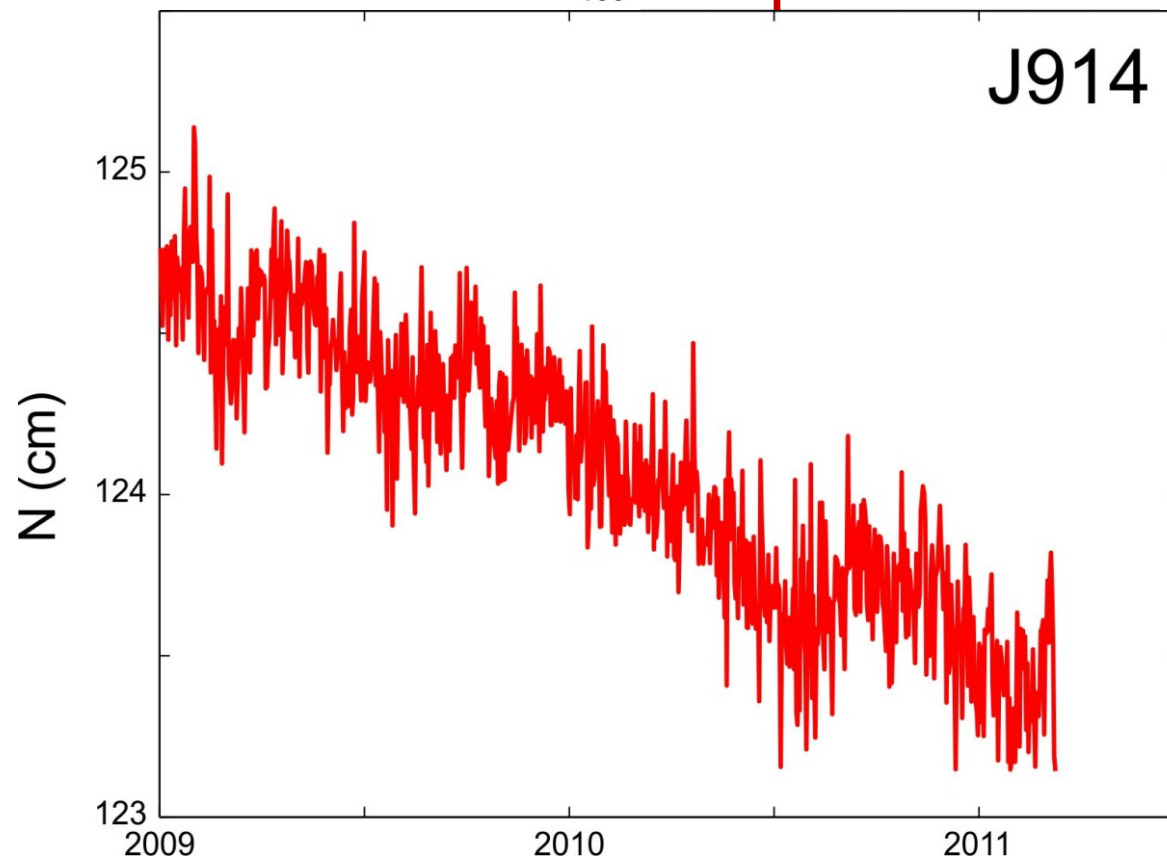
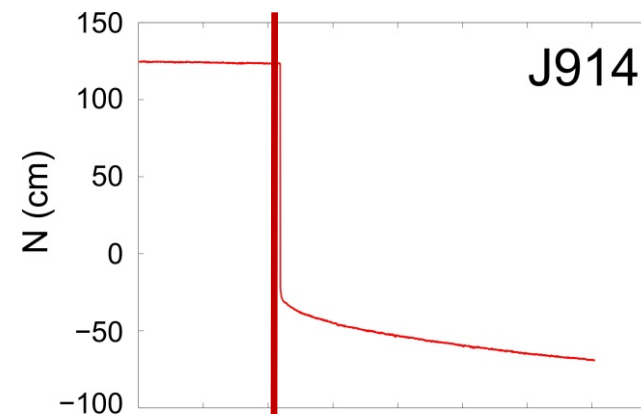
### Up:

Noises:

$$\sigma_{PL} = 10.48 \text{ mm/yr}^{-\kappa/4}, \kappa = -0.40$$

Deterministic part:

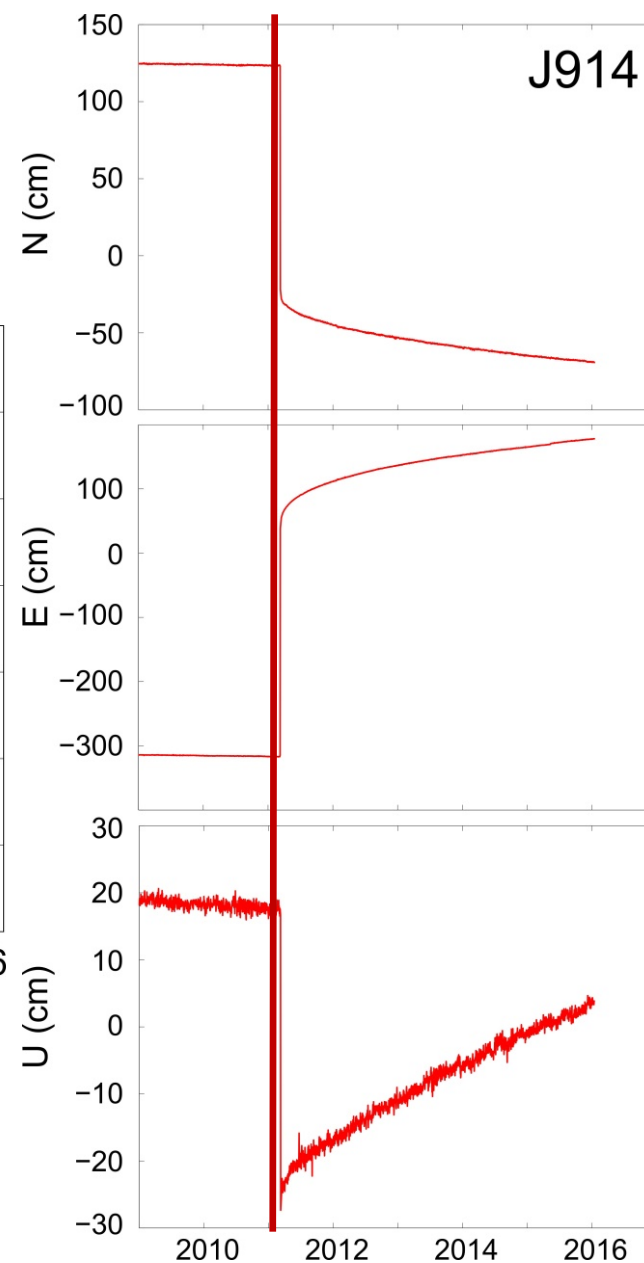
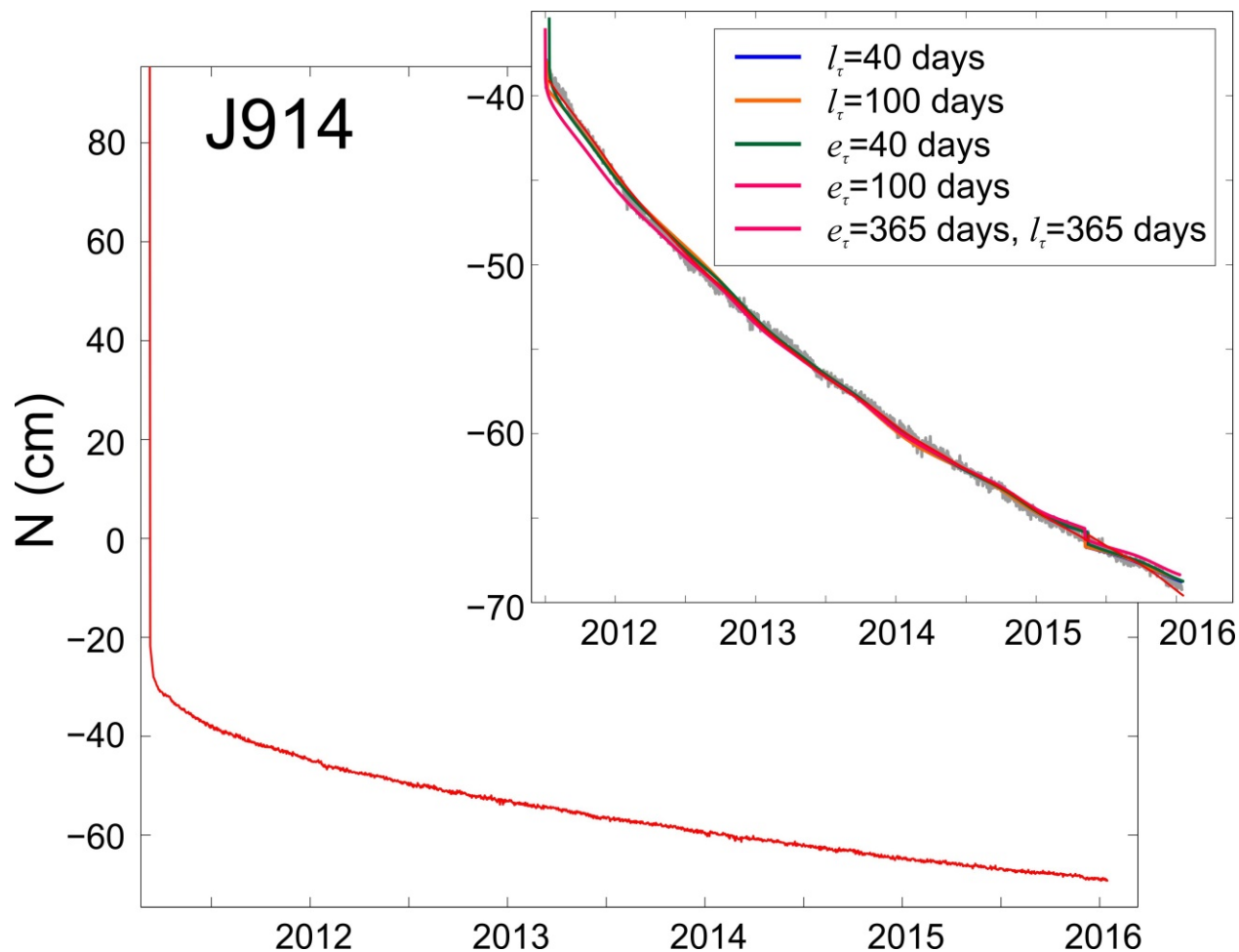
$$v_1 = -3.48 \pm 2.73 \text{ mm/yr}$$



## 6. GNSS data:

### a) Cutting into pieces (after EQ):

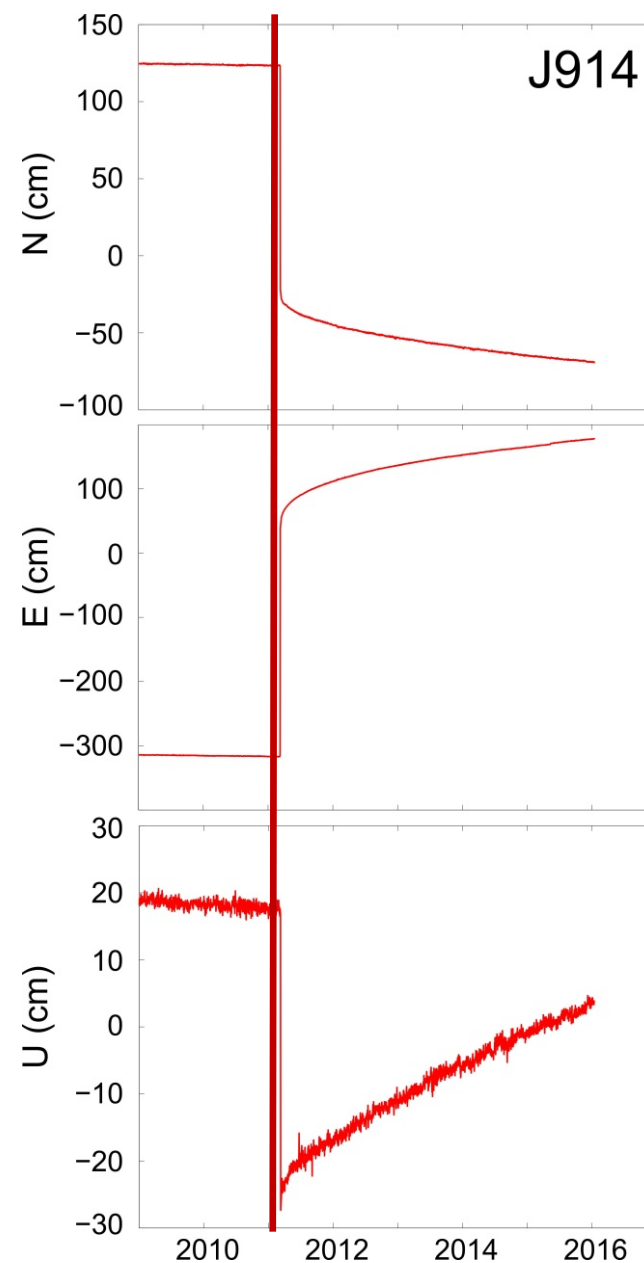
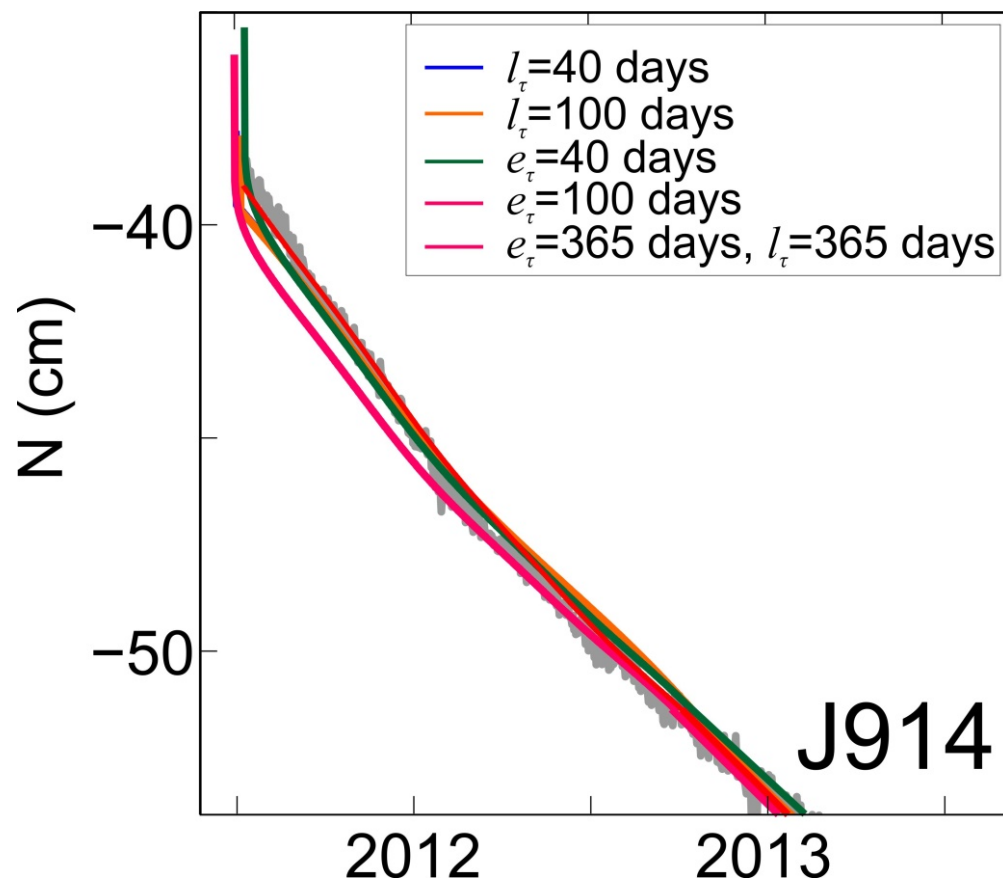
Post-relaxation time ( $e_\tau$  and  $l_\tau$  in days) is a main issue.



## 6. GNSS data:

### a) Cutting into pieces (after EQ):

Post-relaxation time ( $e_\tau$  and  $l_\tau$  in days) is a main issue, AIC and MLF differs a lot.





## 6. GNSS data:

### a) Cutting into pieces (after EHQ):

Post-relaxation time ( $e_\tau$  and  $l_\tau$  in days) is a main issue,

AIC and MLF differs a lot.

#### BEFORE EHQ (North):

Noises:

$$\sigma_{PL} = 2.73 \text{ mm/yr}^{-\kappa/4}, \kappa = -0.36$$

Deterministic part:

$$v_1 = -6.20 \pm 0.72 \text{ mm/yr}$$

#### AFTER EHQ (North):

$$e_\tau = 751, l_\tau = 541$$

(lowest AIC & greatest MLF)

Noises:

$$\sigma_{PL} = 3.97 \text{ mm/yr}^{-\kappa/4}, \kappa = -0.42$$

Deterministic part:

$$v_2 = 148.13 \pm 10.79 \text{ mm/yr}$$

#### BEFORE EHQ (East):

Noises:

$$\sigma_{PL} = 3.01 \text{ mm/yr}^{-\kappa/4}, \kappa = -0.36$$

Deterministic part:

$$v_1 = -14.31 \pm 0.79 \text{ mm/yr}$$

#### AFTER EHQ (East):

$$e_\tau = 421, l_\tau = 1$$

(lowest AIC & greatest MLF)

Noises:

$$\sigma_{PL} = 3.41 \text{ mm/yr}^{-\kappa/4}, \kappa = -0.41$$

Deterministic part:

$$v_2 = 77.81 \pm 1.21 \text{ mm/yr}$$

#### BEFORE EHQ (Up):

Noises:

$$\sigma_{PL} = 10.48 \text{ mm/yr}^{-\kappa/4}, \kappa = -0.40$$

Deterministic part:

$$v_1 = -3.48 \pm 2.73 \text{ mm/yr}$$

#### AFTER EHQ (Up):

$$e_\tau = 1, l_\tau = 511$$

(lowest AIC & greatest MLF)

Noises:

$$\sigma_{PL} = 11.89 \text{ mm/yr}^{-\kappa/4}, \kappa = -0.46$$

Deterministic part:

$$v_2 = 28.92 \pm 2.34 \text{ mm/yr}$$