Discrete Multiscale Modelling and Future Research Plans concerning Metals

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10 yearsPhD, MSc (cum laude), BSc (cum laude)Mechanics of Materials, Mechanical Engineering

Cardiff University (Pierre Kerfriden & Stephane Bordas)

1.5 years Assistant Prof, Institute of Mechanics & Advanced Materials

University of Luxembourg (Hussein Rappel, Jack Hale, Stephane Bordas)

4 months Research Fellow, Computational Mechanics



- 1. Discrete multiscale models for fibrous materials
- Discrete multiscale models for metals 2.
- 3. Future research plans for metals





Fibrous material 1: electronic textile











Fibrous material 1: electronic textile





Fibrous material 1: electronic textile



Fibrous material 2: paper materials



Fibrous material 2: paper materials





Fibrous material 2: paper materials





Quasicontinuum method (Tadmor et al, 1996)



- Ideal for local events in large-scale lattice computations
- Underlying lattice fully resolved where needed
- No continuum/constitutive assumptions





Electronic textile





Results: electronic textile





Failure surfaces





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Results: fiber sliding in paper materials



Results: fiber sliding in paper materials

Horizontal displacement, relative to the uniform displacement



LUXEMBOURG

Lomer di-pole in 2.5D FCC system (EAM)



QC for atomistics



(LJ-potential)



Total number of atoms: Atoms for DOFs: Sampling atoms: 1,074,344 8732 (0.8%) 55,744 (5.1%)



- $\sqrt{\text{Elastoplastic trusses (local dissipative mechanism)}}$
- \sqrt{N} Nodal sliding (non-local dissipative mechanism)
- $\sqrt{\text{Atomistics (conservative but highly nonlocal)}}$
- $\sqrt{\text{Beams}}$
- $\sqrt{1}$ Irregularity
- Adaptivity
- Applications:

1. Technically relevant atomistic problems, 2. Open-cell AI foams with functionally graded Ni coatings.





Open-cell AI foams with functionally graded Ni coatings











(Jung, 2014)

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Open-cell AI foams with functionally graded Ni coatings





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Enhanced discretisation technique for crystal plasticity



(Raabe, 2012)



Advantages:

- 1. Easy remeshing
- 2. Grain boundary fracture
- 3. Growth/shrinkage of crystals

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Multitime modelling for low cycle fatigue of crystal plasticity



(Joseph, 2010)



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Fast Fourier Transformation for RVEs





Resol. N	FFT σ ₀ ^{hom} MPa	CPU time s	Dof's	FEM σ ₀ ^{hom} MPa	CPU time s	400 Fibers 400 Matrix Composite	
16	160.34	1.64	*	*	*	6 ³⁰⁰ / hom	1
32	160.66	3.02	1402	162.36	267.69	200 - <u></u> <u> </u>	
64	160.07	12.21	5710	160.62	2170.28		
128	159.55	53.53	11370	160.37	6464.47	100	1
256	159.29	253.31	*	*	*	0	
512	159.13	1075.60	*	*	*	0.0 0.0025 0.005 0.0	0

(Moulinec & Suquet)



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- $\sqrt{\text{QC}}$ method for dissipative systems (springs/beams, regular/irregular) $\sqrt{\text{QC}}$ method for conservative systems (atomistics)
- QC method for dissipative graded systems (open-cell AI foams)
- Enhanced disretisation technique for crystal plasticity
- Multitime modelling for low cycle fatigue
- FFT modelling for RVEs



Dissipative lattice model based on a Coleman-Noll procedure

Kinematic variables \boldsymbol{u} & history variables \boldsymbol{z} Internal energy $\boldsymbol{E} = \sum_{i=1}^{n} E_i$

Virtual-power $\dot{\boldsymbol{u}}^T \boldsymbol{f}_{int} = \dot{\boldsymbol{u}}^T \boldsymbol{f}_{ext}$ $\forall \dot{\boldsymbol{u}}$ Internal power $P_{int} = \dot{\boldsymbol{E}} + \dot{\boldsymbol{D}}$ Energy rate $\dot{\boldsymbol{E}} = \dot{\boldsymbol{u}}^T \frac{\partial \boldsymbol{E}}{\partial \boldsymbol{u}} + \dot{\boldsymbol{z}}^T \frac{\partial \boldsymbol{E}}{\partial \boldsymbol{z}}$ Dissipation rate $\dot{\boldsymbol{D}} = \dot{\boldsymbol{u}}^T \left(\boldsymbol{f}_{int} - \frac{\partial \boldsymbol{E}}{\partial \boldsymbol{u}} \right) - \dot{\boldsymbol{z}}^T \frac{\partial \boldsymbol{E}}{\partial \boldsymbol{z}} \ge 0$



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Virtual-power-based QC framework

Apply 2 QC reduction steps to

Dissipative lattice model based on a Coleman-Noll procedure

Kinematic variables $\boldsymbol{u} = \Psi \boldsymbol{\overline{u}}$ & history variables \boldsymbol{z} Internal energy $\boldsymbol{E} = \sum_{i \in S} E_i$

Virtual-power
$$\dot{\overline{u}}^T \Psi^T f_{int} = \dot{\overline{u}}^T \Psi^T f_{ext}$$
 $\forall \dot{\overline{u}}$ Internal power $P_{int} = \dot{E} + \dot{D}$ Energy rate $\dot{E} = \dot{\overline{u}}^T \Psi^T \frac{\partial E}{\partial u} + \dot{z}^T \frac{\partial E}{\partial z}$ Dissipation rate $\dot{D} = \dot{\overline{u}}^T \left(f_{int} - \Psi^T \frac{\partial E}{\partial u} \right) - \dot{z}^T \frac{\partial E}{\partial z} \ge 0$
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Virtual-power-based QC framework





Electronic textile





Electronic textile



Results: electronic textile





Failure surfaces





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